

# HUMANITY

Series of PowerPoint Presentations by J. W. Gardner

- Misbeliefs – Acquisition & Probable Examples
- Big Picture Science – Observable Universe
- Big Picture Science – Planet Earth
- Big Picture Science – Life on Earth
- Basic Science Sampler – Quantum Physics, Relativistic Physics and Thermodynamics



# Quantum Physics

Double-slit experiment

Entanglement

Periodic Table

Standard Model

## Special Relativity

Relativity of time interval -- Hafele-Keating -- Slowing of time by gravity

Relativity of length

Nonlinear speed addition

Relativity of simultaneity

Relativistic dynamics

## General Relativity

Bending of light

Black holes

Gravitoelectromagnetism

Gravitational waves

## Thermodynamics

First and second laws

Entropy generation

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# Double-Slit Experiment

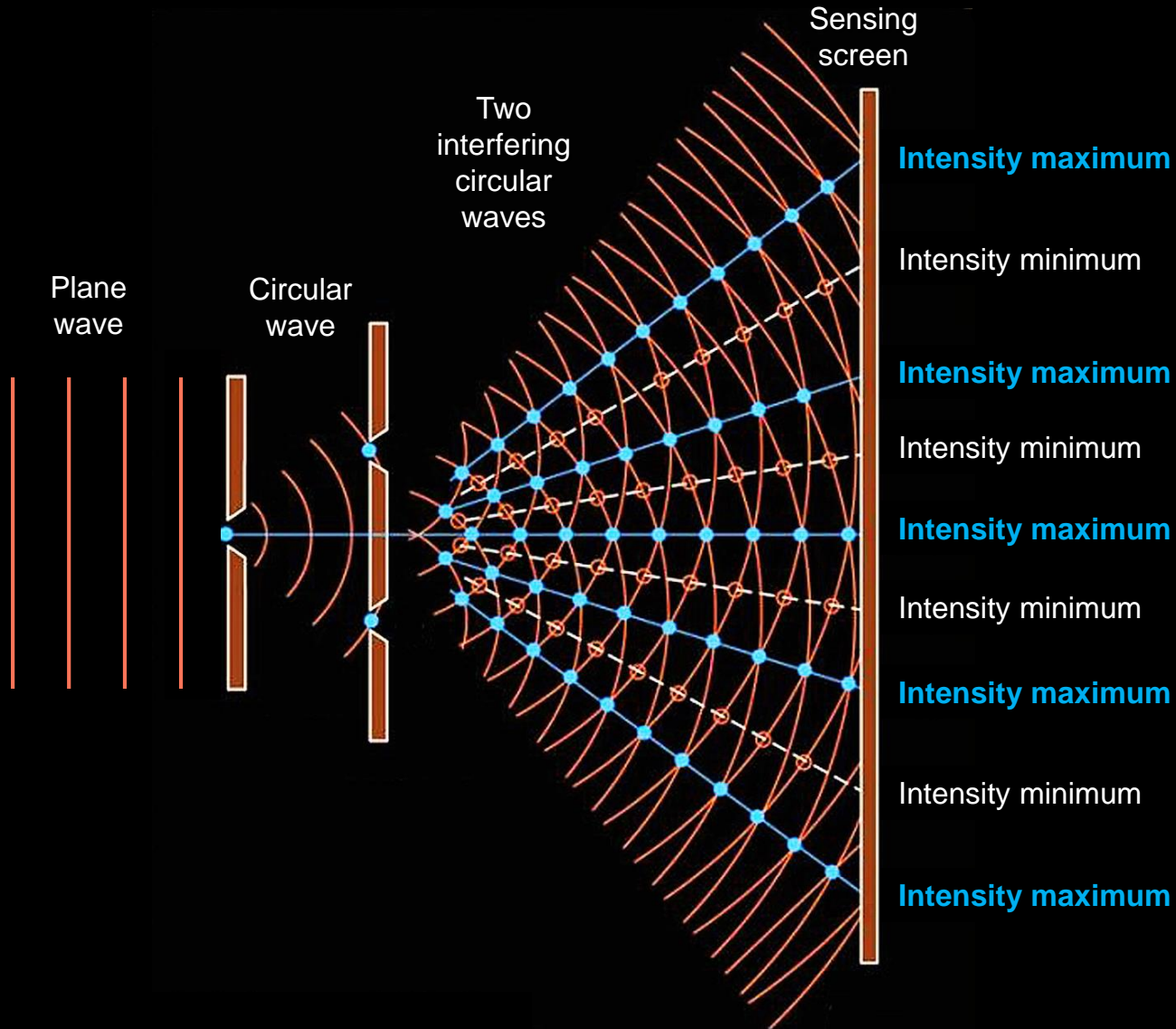
Experiment with Light

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Oldest type demonstrates wave nature of light in form of interference bands

Light also can exhibit particle-like behavior, as in photoelectric effect

# Double-Slit Experiment with Light



Light intensity maximums and minimums resulting from constructive and destructive wave interference. Similar experiment first done by Thomas Young in 1803. Same behavior exhibited by water waves in pan

# **Double-Slit Experiment**

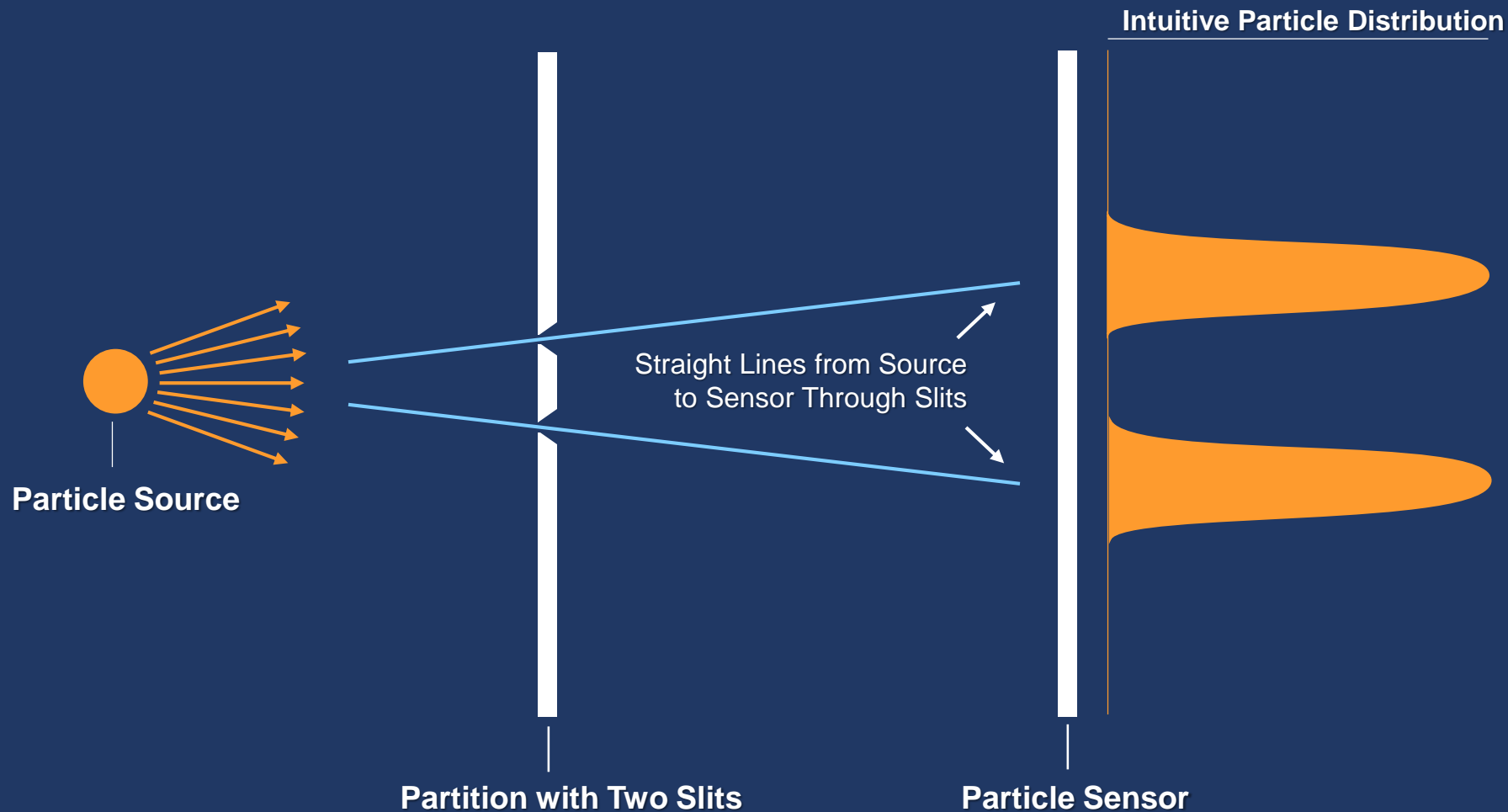
Experiment with Massive Particles

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**Counterintuitively, experiment with massive particles also reveals interference bands**

# Double Slit Experiment with Massive Particles

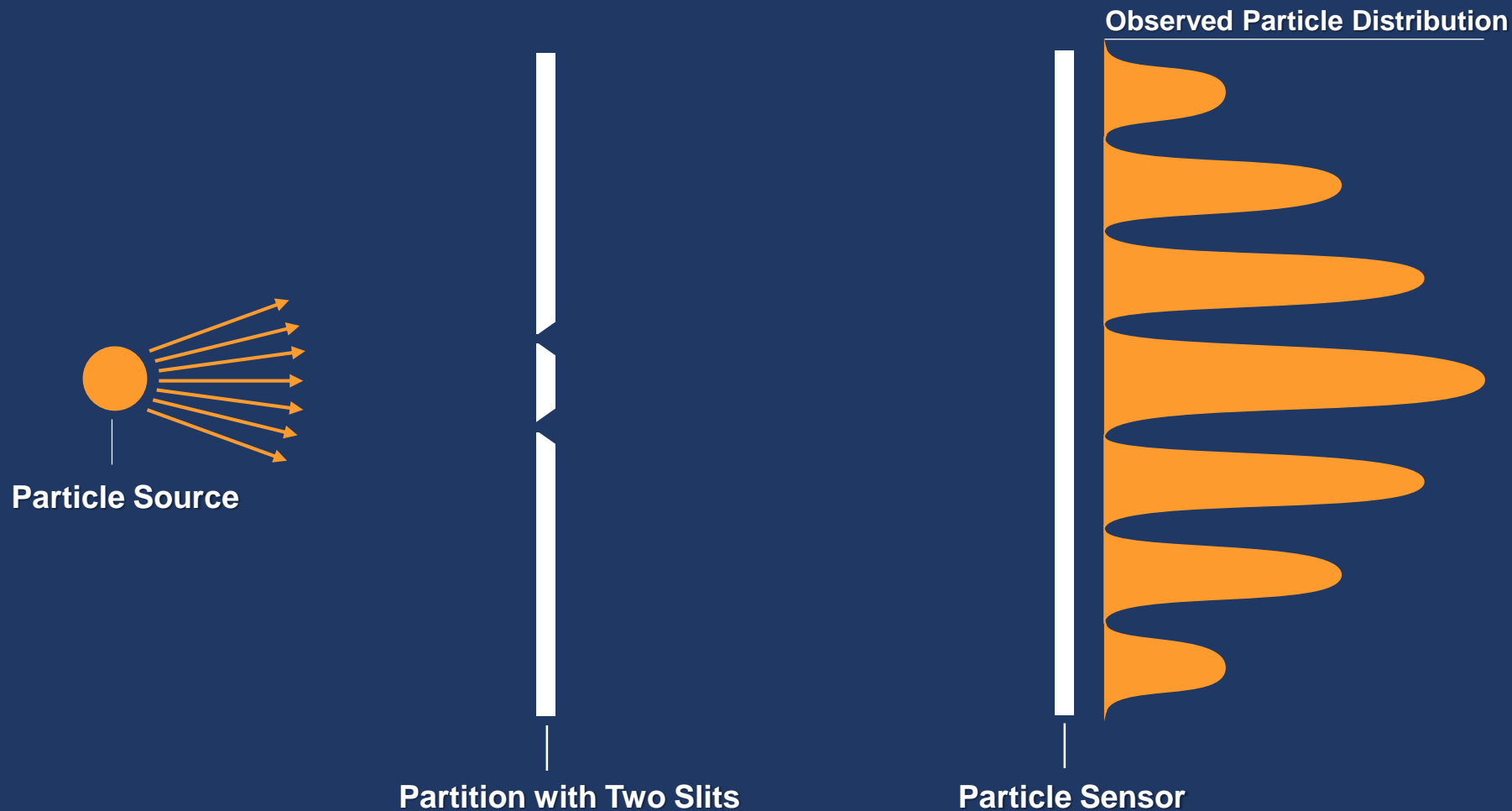
Intuitive (Classical) Expectation for Particles Is No Interference





# Double Slit Experiment with Massive Particles

Actual Result = Quantum Mechanical Prediction (Wave Interference Pattern)



Observed with electrons and with molecules containing as many 70 carbon atoms (perhaps more)

# Double-Slit Experiment

Monitor Particles Exiting One Slit

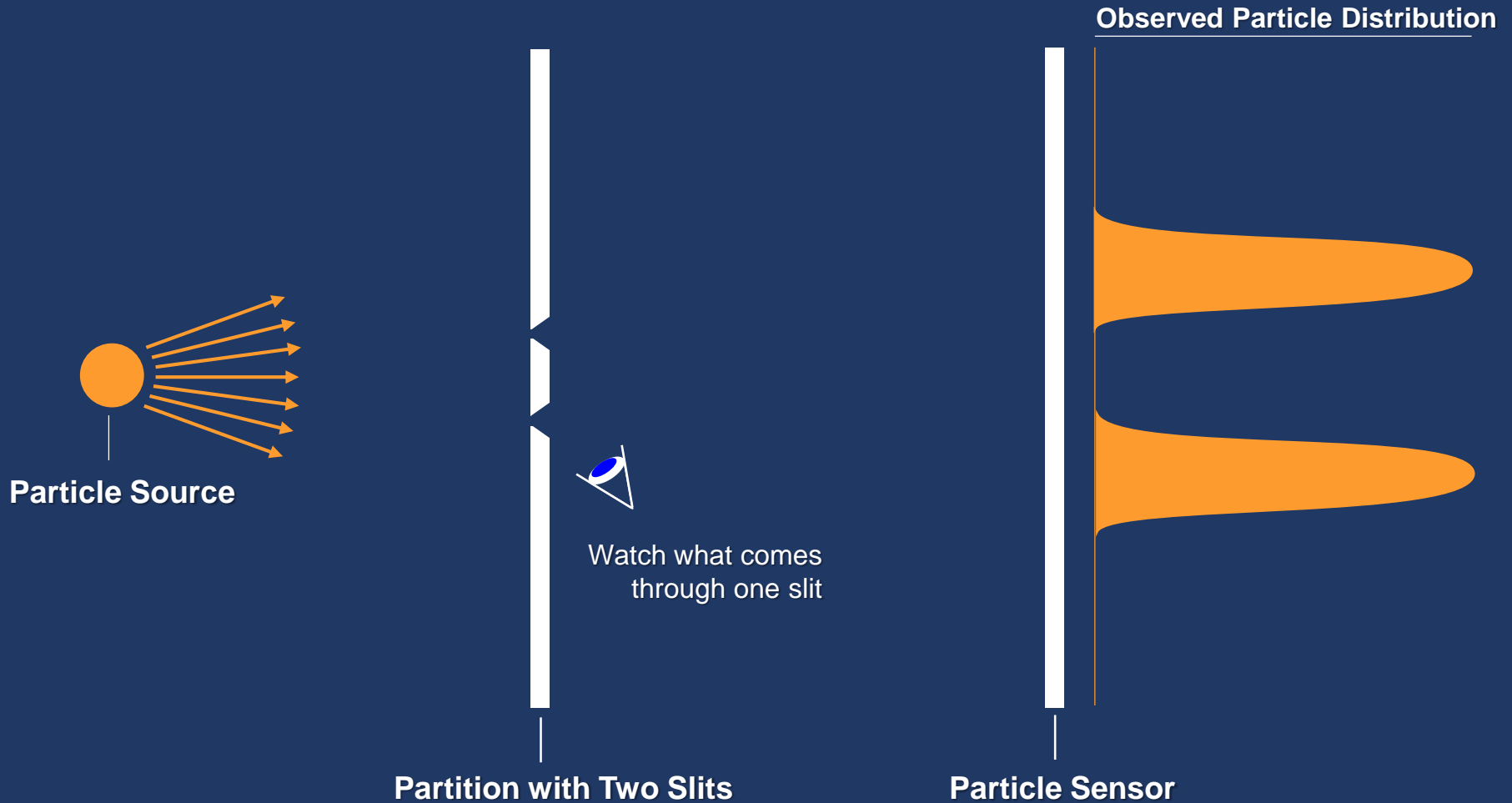
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**Not surprisingly, perhaps, monitoring particles exiting one slit eliminates interference pattern**

Not surprising because act of observation alters system

# Double Slit Experiment with Massive Particles

Watch What Comes Through One Slit



If what comes through either slit is observed then classical result is obtained

# Double-Slit Experiment

One Particle at a Time

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More counterintuitive is what happens if the experiment is done one particle at a time

# Tonomura Double-Slit Experiment with Individual Electrons

Screen now in plane of slide. Each electron hit recorded before next fired



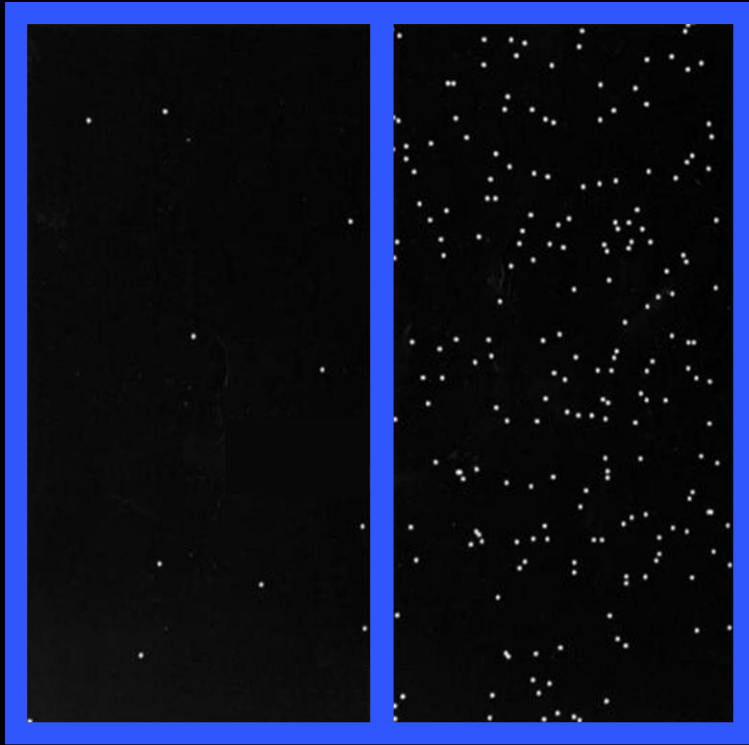
Increasing Time



"Demonstration of single-electron buildup of an interference pattern," Tonomura, et al, *Am. J. Phys.* 57, 117 (1989)

# Tonomura Double-Slit Experiment with Individual Electrons

Screen now in plane of slide. Each electron hit recorded before next fired



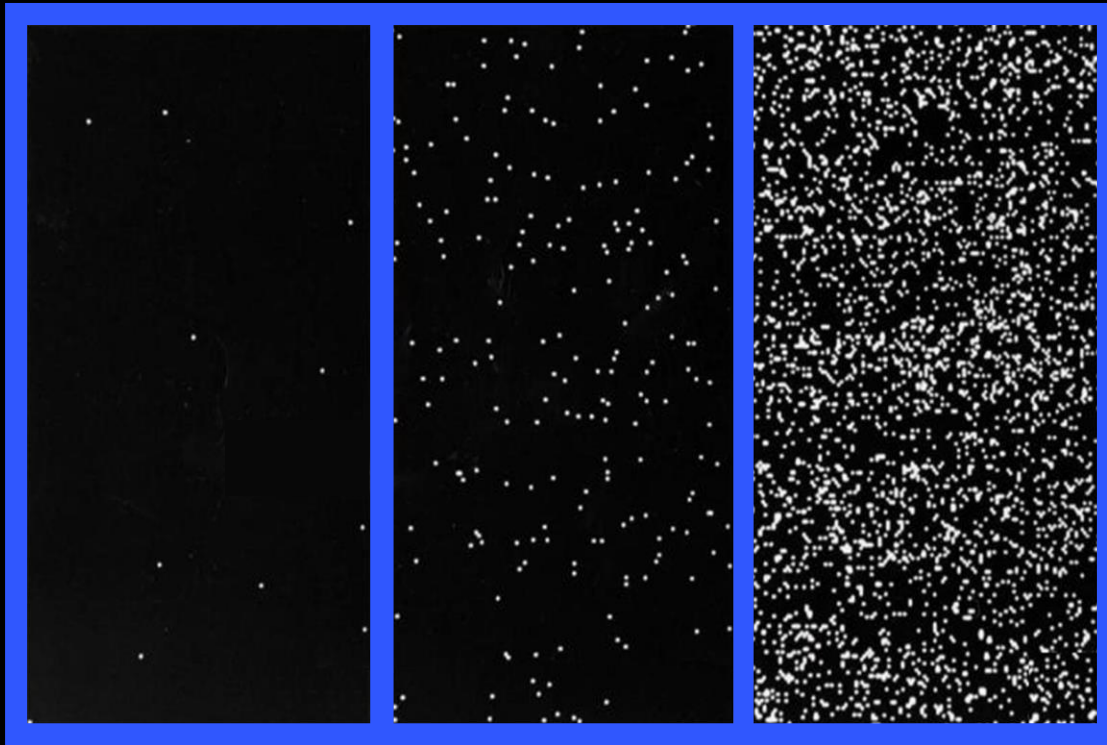
Increasing Time



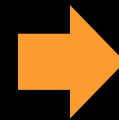
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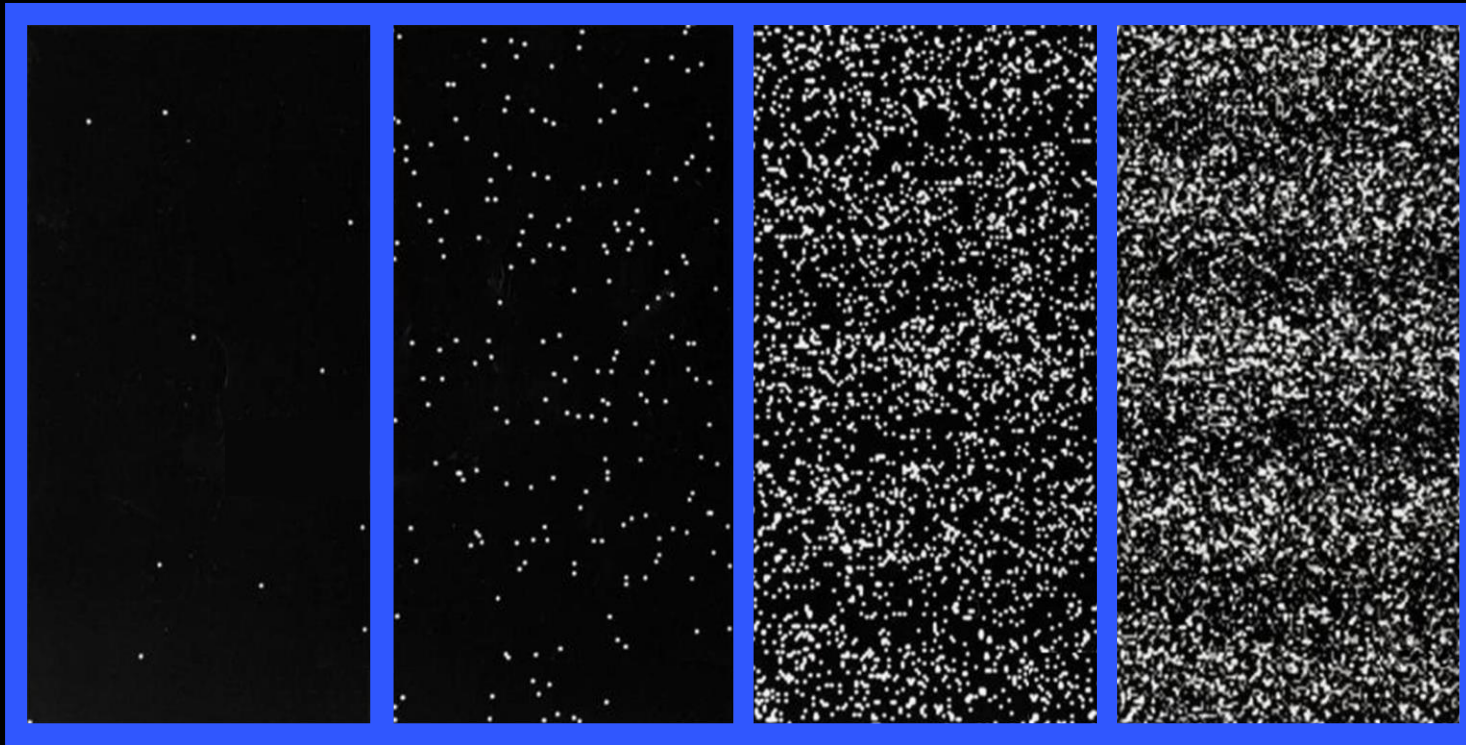
Increasing Time



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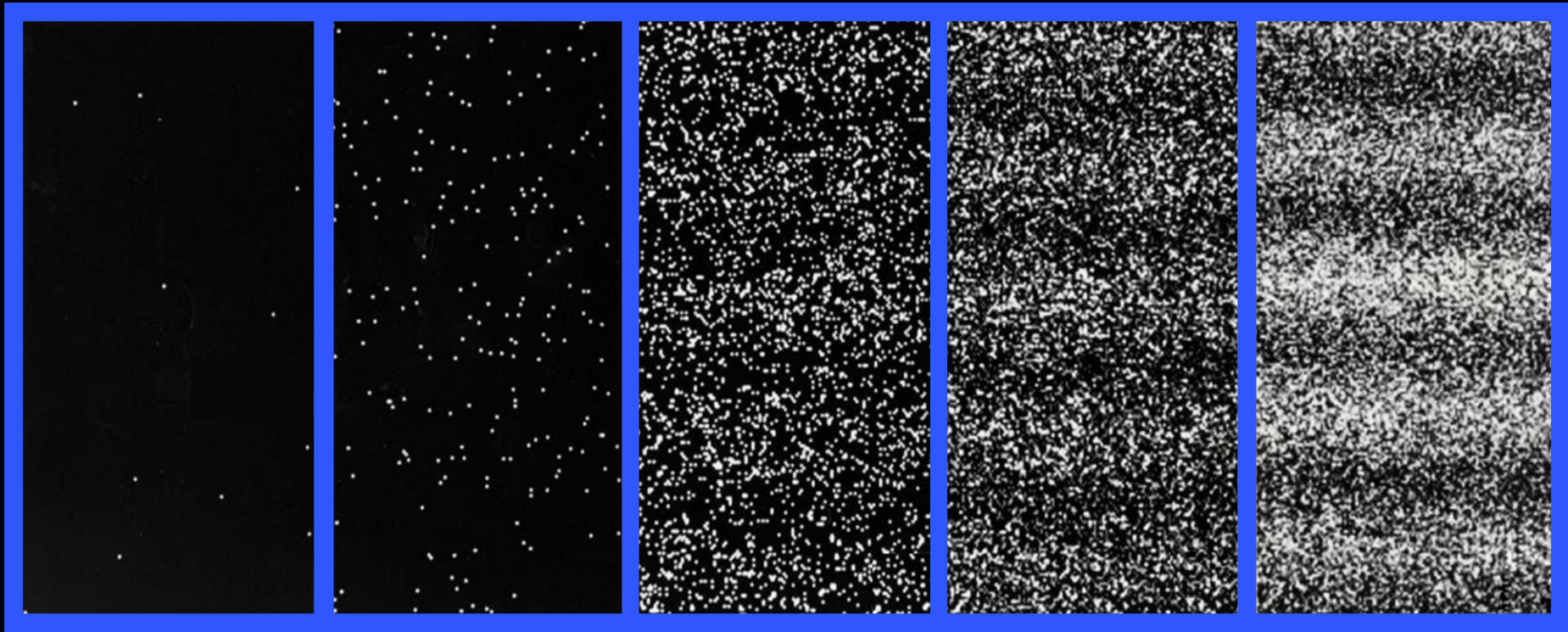


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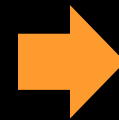


# Tonomura Double-Slit Experiment with Individual Electrons

Screen now in plane of slide. Each electron hit recorded before next fired



Increasing Time



"Demonstration of single-electron buildup of an interference pattern," Tonomura, et al, *Am. J. Phys.* 57, 117 (1989)

Last experiment emphasizes the probabilistic nature of quantum mechanics

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# Quantum Entanglement

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- **Limbo-like state in which two particles are linked over arbitrary distances and property values are undetermined**
- **Measuring a property value of one particle breaks entanglement, whence other particle manifests complimentary value**
- **Quantum mechanics places no limit on rate of manifestation**

Laser pulses, for example, have been used to entangle photons of different polarity and electrons of different spin

# Quantum Entanglement

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- **Quantum mechanics places no limit on rate of manifestation**

That required to satisfy some conservation principle

# Quantum Entanglement

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- **Measuring a property value of one particle breaks entanglement, whence other particle manifests complimentary value**
- **Quantum mechanics places no limit on rate of manifestation**

Manifestation times less than  $1/10,000$  of light transit time between particles have been observed

## **Quantum Entanglement: Einstein's "Spooky Action at a Distance"**

*It has now been shown that either causal influences propagate faster than light, or a common-sense notion about what the word "cause" signifies is wrong*

– Howard Wiseman (2015)\*

\*Writing in reference to experiments by Henson, et al (2015) "Experimental loophole-free violation of a Bell inequality using entangled electron spins separated by 1.3 km" arXiv:1508.05949



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# Periodic Table of Elements

---

- **Table organizing 118 discovered elements. The standard version is based on atomic number, electron configuration & recurring chemical properties**
- **One alternative is based solely on quantum numbers associated with the solution of the Schrödinger equation for a single electron orbiting a nucleus**

# Standard Periodic Table

Found on Walls of Chemistry Classrooms & Labs

1 H Hydrogen																	2 He Helium
3 Li Lithium	4 Be Beryllium											5 B Boron	6 C Carbon	7 N Nitrogen	8 O Oxygen	9 F Fluorine	10 Ne Neon
11 Na Sodium	12 Mg Magnesium											13 Al Aluminium	14 Si Silicon	15 P Phosphorus	16 S Sulfur	17 Cl Chlorine	18 Ar Argon
19 K Potassium	20 Ca Calcium	21 Sc Scandium	22 Ti Titanium	23 V Vanadium	24 Cr Chromium	25 Mn Manganese	26 Fe Iron	27 Co Cobalt	28 Ni Nickel	29 Cu Copper	30 Zn Zinc	31 Ga Gallium	32 Ge Germanium	33 As Arsenic	34 Se Selenium	35 Br Bromine	36 Kr Krypton
37 Rb Rubidium	38 Sr Strontium	39 Y Yttrium	40 Zr Zirconium	41 Nb Niobium	42 Mo Molybdenum	43 Tc Technetium	44 Ru Ruthenium	45 Rh Rhodium	46 Pd Palladium	47 Ag Silver	48 Cd Cadmium	49 In Indium	50 Sn Tin	51 Sb Antimony	52 Te Tellurium	53 I Iodine	54 Xe Xenon
55 Cs Cesium	56 Ba Barium	57-71 La-Lu Lanthanides	72 Hf Hafnium	73 Ta Tantalum	74 W Tungsten	75 Re Rhenium	76 Os Osmium	77 Ir Iridium	78 Pt Platinum	79 Au Gold	80 Hg Mercury	81 Tl Thallium	82 Pb Lead	83 Bi Bismuth	84 Po Polonium	85 At Astatine	86 Rn Radon
87 Fr Francium	88 Ra Radium	89-103 Ac-Lr Actinides	104 Rf Rutherfordium	105 Db Dubnium	106 Sg Seaborgium	107 Bh Bohrium	108 Hs Hassium	109 Mt Meitnerium	110 Ds Darmstadtium	111 Rg Roentgenium	112 Cn Copernicium	113 Nh Nihonium	114 Fl Flerovium	115 Mc Moscovium	116 Lv Livermorium	117 Ts Tennessine	118 Og Oganesson

57 La Lanthanum	58 Ce Cerium	59 Pr Praseodymium	60 Nd Neodymium	61 Pm Promethium	62 Sm Samarium	63 Eu Europium	64 Gd Gadolinium	65 Tb Terbium	66 Dy Dysprosium	67 Ho Holmium	68 Er Erbium	69 Tm Thulium	70 Yb Ytterbium	71 Lu Lutetium
89 Ac Actinium	90 Th Thorium	91 Pa Protactinium	92 U Uranium	93 Np Neptunium	94 Pu Plutonium	95 Am Americium	96 Cm Curium	97 Bk Berkelium	98 Cf Californium	99 Es Einsteinium	100 Fm Fermium	101 Md Mendelevium	102 No Nobelium	103 Lr Lawrencium

Numbers in boxes are atomic numbers (numbers of protons in nucleus). Columns consist of elements with similar properties. From Scientific Gems - WordPress.com

# Periodic Table of Elements

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- **Table organizing 118 discovered elements. The standard version is based on atomic number, electron configuration & recurring chemical properties**
- **One alternative is based solely on quantum numbers associated with the solution of the Schrödinger equation for a single electron orbiting a nucleus**

The particular such alternative considered here is the left-step table of Charles Janet

# Quantum Mechanics of Hydrogen Atom

## Time-independent Schrödinger equation for electron

$$E\psi = \left[ \frac{-\hbar^2}{2\mu} \nabla^2 - \frac{e^2}{4\pi\epsilon_0 r} \right] \psi$$

## Solution in spherical coordinates

$$\psi_{nlm}(r, \theta, \phi) = \sqrt{\left(\frac{\rho}{r}\right)^3 \frac{(n-l-1)!}{2n(n+l)!}} e^{-\rho/2} \rho^l L_{n-l-1}^{2l+1}(\rho) Y_l^m(\theta, \phi)$$

$E$  = energy,  $\psi$  = wave function,  $\hbar$  = reduced Planck constant,  $\mu$  = reduced mass =  $m_e m_p / (m_e + m_p)$   
 $m_e$  = electron mass,  $m_p$  = proton mass,  $e$  = charge magnitude of electron and proton,  
 $\epsilon_0$  = dielectric constant,  $r$  = distance from center of proton,  $n$  = principal quantum number,  
 $l$  = azimuthal quantum number,  $m$  = magnetic quantum number,  $\rho = 2r/(na_0)$ ,  
 $a_0$  = Bohr radius =  $4\pi\epsilon_0\hbar^2/m_e e^2$ ,  $L_{n-l-1}^{2l+1}(\rho)$  = Laguerre polynomial,  $Y_l^m(\theta, \phi)$  = spherical harmonic

# Meaning of Quantum Numbers

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- Principal quantum number  $n$  linked to energy level of electron orbital, with values 1, 2, 3 . . .
- Azimuthal quantum number  $\ell$  linked to orbital angular momentum of electron, with values 0, 1, 2 . . .  $n - 1$ ,
- Magnetic quantum number  $m$  linked to magnetic moment of electron, with values  $-\ell, -(\ell - 1) \dots - 1, 0, 1 \dots \ell - 1, \ell$
- Spin quantum number  $m_s$  linked to "orientation" of electron spin, with values  $+\frac{1}{2}$  or  $-\frac{1}{2}$

Note that the wave function  $\psi$  is not dimensionless,  
but has units of  $\text{length}^{-3/2}$

Consequently, the probability density (next slide) has units of reciprocal volume

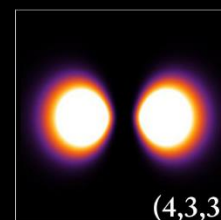
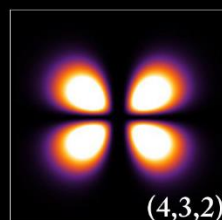
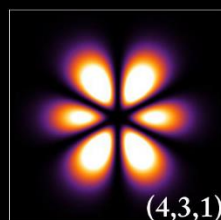
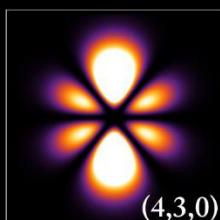
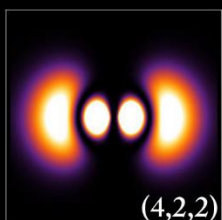
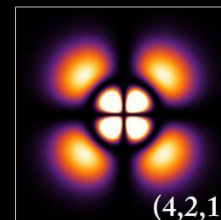
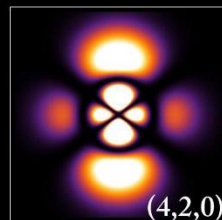
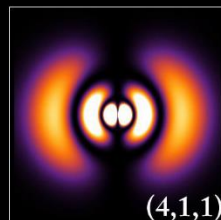
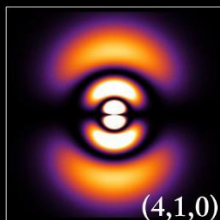
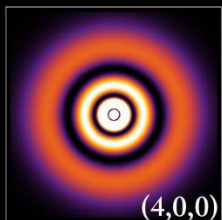
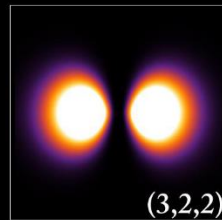
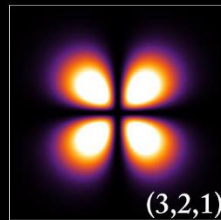
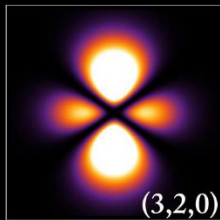
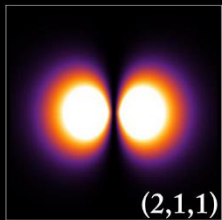
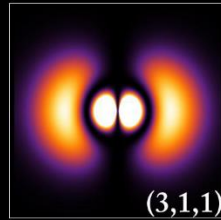
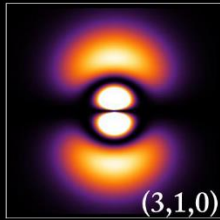
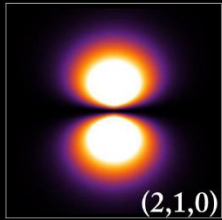
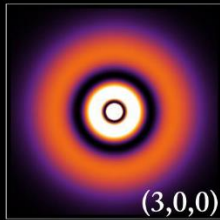
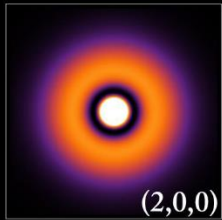
# Hydrogen Atom Orbitals

## Electron Probability Densities

$n$  = principal quantum number

$l$  = azimuthal quantum number

$m$  = magnetic quantum number



$(n, l, m)$



Note also that atoms are mostly empty space. If the entire atom were the size of a baseball stadium, the nucleus, where essentially all the mass is concentrated, would be the size of a peanut

# Conversion of Standard Table to Janet Table

The diagram illustrates the conversion of the standard periodic table to the Janet periodic table. The standard table is shown at the top, and the Janet table is shown at the bottom. A pink arrow labeled '1' indicates the movement of Helium (He) from its original position to the position of Hydrogen (H). A pink arrow labeled '2' indicates the movement of the f-block (lanthanides and actinides) from its original position to the bottom of the table. A pink arrow labeled '3' indicates the movement of the f-block from the bottom to the left side of the Janet table.

1 H Hydrogen																	2 He Helium
3 Li Lithium	4 Be Beryllium											5 B Boron	6 C Carbon	7 N Nitrogen	8 O Oxygen	9 F Fluorine	10 Ne Neon
11 Na Sodium	12 Mg Magnesium											13 Al Aluminium	14 Si Silicon	15 P Phosphorus	16 S Sulfur	17 Cl Chlorine	18 Ar Argon
19 K Potassium	20 Ca Calcium	21 Sc Scandium	22 Ti Titanium	23 V Vanadium	24 Cr Chromium	25 Mn Manganese	26 Fe Iron	27 Co Cobalt	28 Ni Nickel	29 Cu Copper	30 Zn Zinc	31 Ga Gallium	32 Ge Germanium	33 As Arsenic	34 Se Selenium	35 Br Bromine	36 Kr Krypton
37 Rb Rubidium	38 Sr Strontium	39 Y Yttrium	40 Zr Zirconium	41 Nb Niobium	42 Mo Molybdenum	43 Tc Technetium	44 Ru Ruthenium	45 Rh Rhodium	46 Pd Palladium	47 Ag Silver	48 Cd Cadmium	49 In Indium	50 Sn Tin	51 Sb Antimony	52 Te Tellurium	53 I Iodine	54 Xe Xenon
55 Cs Cesium	56 Ba Barium	57-71 La-Lu Lanthanides	72 Hf Hafnium	73 Ta Tantalum	74 W Tungsten	75 Re Rhenium	76 Os Osmium	77 Ir Iridium	78 Pt Platinum	79 Au Gold	80 Hg Mercury	81 Tl Thallium	82 Pb Lead	83 Bi Bismuth	84 Po Polonium	85 At Astatine	86 Rn Radon
87 Fr Francium	88 Ra Radium	89-103 Ac-Lr Actinides	104 Rf Rutherfordium	105 Db Dubnium	106 Sg Seaborgium	107 Bh Bohrium	108 Hs Hassium	109 Mt Meitnerium	110 Ds Darmstadtium	111 Rg Roentgenium	112 Cn Copernicium	113 Nh Nihonium	114 Fl Flerovium	115 Mc Moscovium	116 Lv Livermorium	117 Ts Tennessine	118 Og Oganesson
57 La Lanthanum	58 Ce Cerium	59 Pr Praseodymium	60 Nd Neodymium	61 Pm Promethium	62 Sm Samarium	63 Eu Europium	64 Gd Gadolinium	65 Tb Terbium	66 Dy Dysprosium	67 Ho Holmium	68 Er Erbium	69 Tm Thulium	70 Yb Ytterbium	71 Lu Lutetium			
89 Ac Actinium	90 Th Thorium	91 Pa Protactinium	92 U Uranium	93 Np Neptunium	94 Pu Plutonium	95 Am Americium	96 Cm Curium	97 Bk Berkelium	98 Cf Californium	99 Es Einsteinium	100 Fm Fermium	101 Md Mendelevium	102 No Nobelium	103 Lr Lawrencium			

# Charles Janet Left-Step Periodic Table (1929)

$\ell = 3$

$\ell = 2$

$\ell = 1$

$\ell = 0$

f

d

p

s

Block letters f, d, p and s correspond to values of azimuthal quantum number  $\ell$

Magnetic quantum number  $m$  varies along each row of a block

1 H  
2 He  
3 Li  
4 Be

5 B 6 C 7 N 8 O 9 F 10 Ne  
11 Na 12 Mg  
13 Al 14 Si 15 P 16 S 17 Cl 18 Ar  
19 K 20 Ca

21 Sc 22 Ti 23 V 24 Cr 25 Mn 26 Fe 27 Co 28 Ni 29 Cu 30 Zn  
31 Ga 32 Ge 33 As 34 Se 35 Br 36 Kr  
37 Rb 38 Sr  
39 Y 40 Zr 41 Nb 42 Mo 43 Tc 44 Ru 45 Rh 46 Pd 47 Ag 48 Cd  
49 In 50 Sn 51 Sb 52 Te 53 I 54 Xe  
55 Cs 56 Ba

57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	87 Fr	88 Ra
89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og	119	120

1s  
2s  
3s  
4s  
5s  
6s  
7s  
8s

2p  
3p  
4p  
5p  
6p  
7p

3d  
4d  
5d  
6d

4f  
5f

Block row number. Equal to value of principal quantum number  $n$

Quantum numbers here apply to the outermost or valence electron of each element

For most elements, the electron configuration can be read directly from the Janet Table. In the case of **sulfur**, for example, the configuration is **1s<sup>2</sup> 2s<sup>2</sup> 2p<sup>6</sup> 3s<sup>2</sup> 3p<sup>4</sup>** (read left to right, row by row, starting with hydrogen)

$\ell = 3$

$\ell = 2$

$\ell = 1$

$\ell = 0$

f

d

p

s

Block letters f, d, p and s correspond to values of azimuthal quantum number  $\ell$

Magnetic quantum number  $m$  varies along each row of a block

1s<sup>2</sup>

2s<sup>2</sup>

2p<sup>6</sup>3s<sup>2</sup>

3p<sup>4</sup>

1 H 2 He

3 Li 4 Be

5 B	6 C	7 N	8 O	9 F	10 Ne	11 Na	12 Mg
-----	-----	-----	-----	-----	-------	-------	-------

13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	19 K	20 Ca
-------	-------	------	------	-------	-------	------	-------

21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	37 Rb	38 Sr
-------	-------	------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------

39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	55 Cs	56 Ba
------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	------	-------	-------	-------

57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	87 Fr	88 Ra
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89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og	119	120
-------	-------	-------	------	-------	-------	-------	-------	-------	-------	-------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	--------	-----	-----

1s

2s

3s

4s

5s

6s

7s

8s

2p

3p

4p

5p

6p

7p

3d

4d

5d

6d

4f

5f

Block row number. Equal to value of principal quantum number  $n$

Because some energy levels are quite close, reading the electron configuration directly from the Janet table does not always work, as with Cr, Cu, Nb, Mo, Ru, Rh, Pd, Ag, La, Gd, Pt, Au, Ac, Th, Pa, U and Cm (highlighted by yellow borders below)\*

$\ell = 3$

$\ell = 2$

$\ell = 1$

$\ell = 0$

f

d

p

s

Block letters f, d, p and s correspond to values of azimuthal quantum number  $\ell$

Magnetic quantum number  $m$  varies along each row of a block

1  
H  
2  
He  
3  
Li  
4  
Be

5  
B  
6  
C  
7  
N  
8  
O  
9  
F  
10  
Ne  
11  
Na  
12  
Mg  
13  
Al  
14  
Si  
15  
P  
16  
S  
17  
Cl  
18  
Ar  
19  
K  
20  
Ca

21  
Sc  
22  
Ti  
23  
V  
24  
Cr  
25  
Mn  
26  
Fe  
27  
Co  
28  
Ni  
29  
Cu  
30  
Zn  
31  
Ga  
32  
Ge  
33  
As  
34  
Se  
35  
Br  
36  
Kr  
37  
Rb  
38  
Sr  
39  
Y  
40  
Zr  
41  
Nb  
42  
Mo  
43  
Tc  
44  
Ru  
45  
Rh  
46  
Pd  
47  
Ag  
48  
Cd  
49  
In  
50  
Sn  
51  
Sb  
52  
Te  
53  
I  
54  
Xe  
55  
Cs  
56  
Ba

57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	87 Fr	88 Ra
89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og	119	120

1s  
2s  
3s  
4s  
5s  
6s  
7s  
8s

2p  
3p  
4p  
5p  
6p  
7p

3d  
4d  
5d  
6d

4f  
5f

Block row number. Equal to value of principal quantum number  $n$

\*From "The Periodic Table of the Elements" on Albert Tarantola's web page

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Relativity of simultaneity

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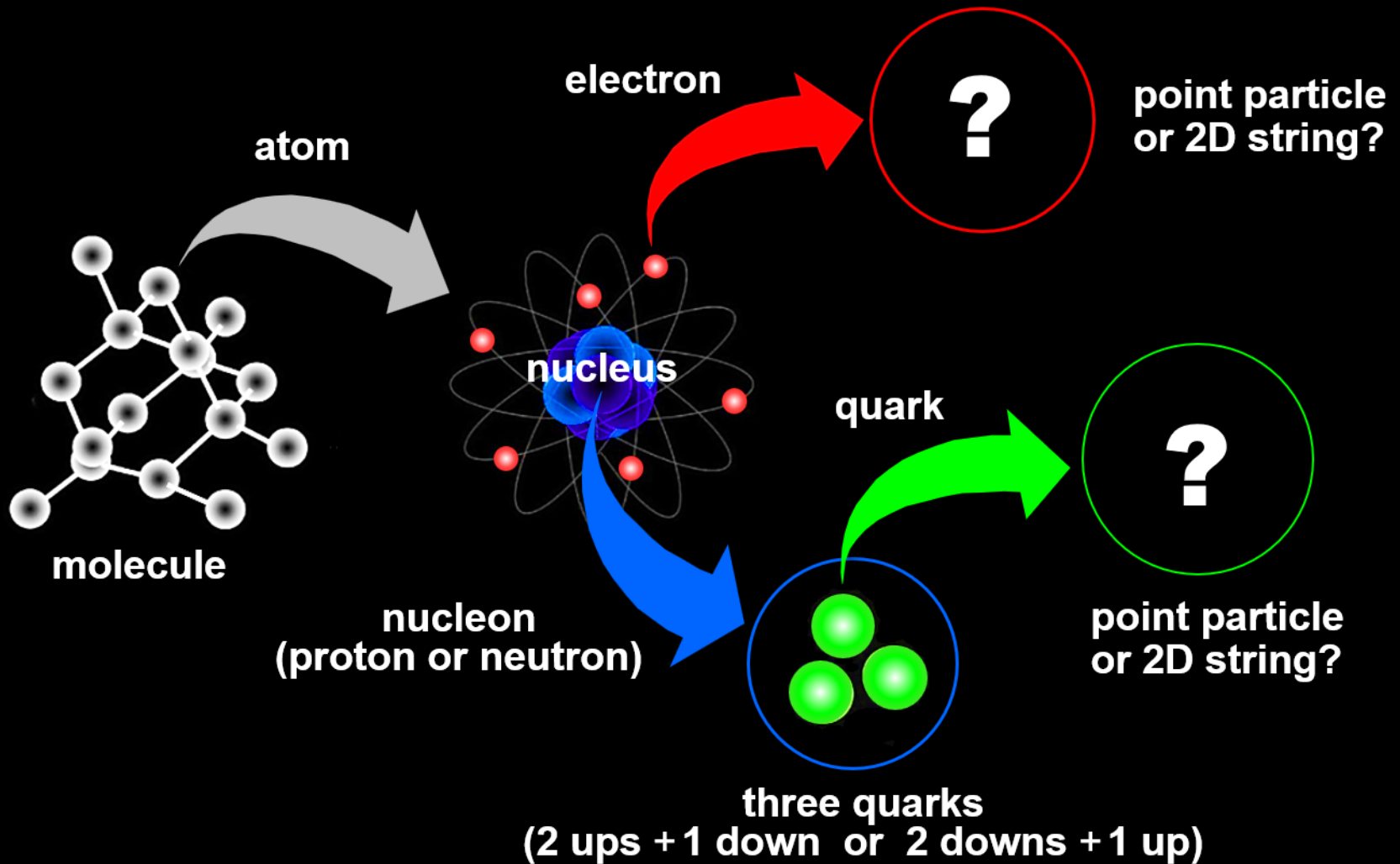
Entropy generation

# Standard Model of Particle Physics

---

- **Currently most fundamental and comprehensive theory of the world supported by laboratory experiments**
- **Describes three of the four known fundamental forces of nature (electromagnetic, weak and strong nuclear, but not gravity) as exchanges of mediating particles (bosons) between matter particles (quarks and leptons, known collectively as fermions)**
- **Loose combination of two quantum field theories: electroweak theory and quantum chromodynamics**
- **As a quantum field theory, adopts the flat spacetime of special relativity**
- **Also excludes dark matter and dark energy, which are important in cosmology, but have yet to be linked to observable particles**

# Inside Molecules





More fundamental particles than electrons  
and up/down quarks have been observed  
in particle colliders

# Fundamental Particles

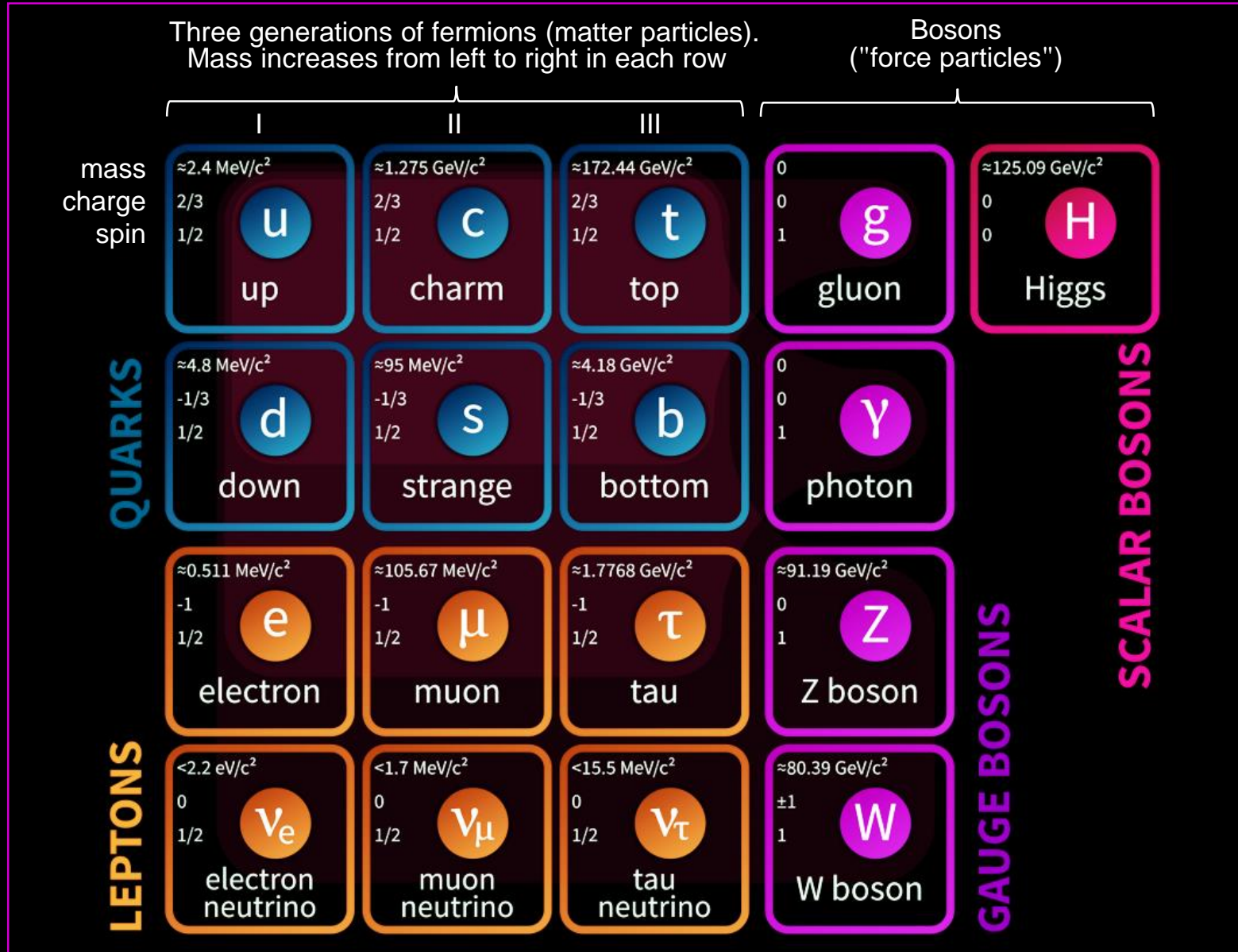
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- Fermions – Matter particles
- Bosons – "Force particles"

Fermions are spin  $1/2$  particles (masses and charges vary). Gauge bosons are spin 0 particles (masses and charges vary). The other boson is the Higgs (massive; spin and charge both 0)

# Standard Model of Particle Physics

## Fundamental Particles and Properties



Whether standard model particles are points, 2D strings or something else is unknown. Image: Wikipedia "Standard Model" article (modified slightly)

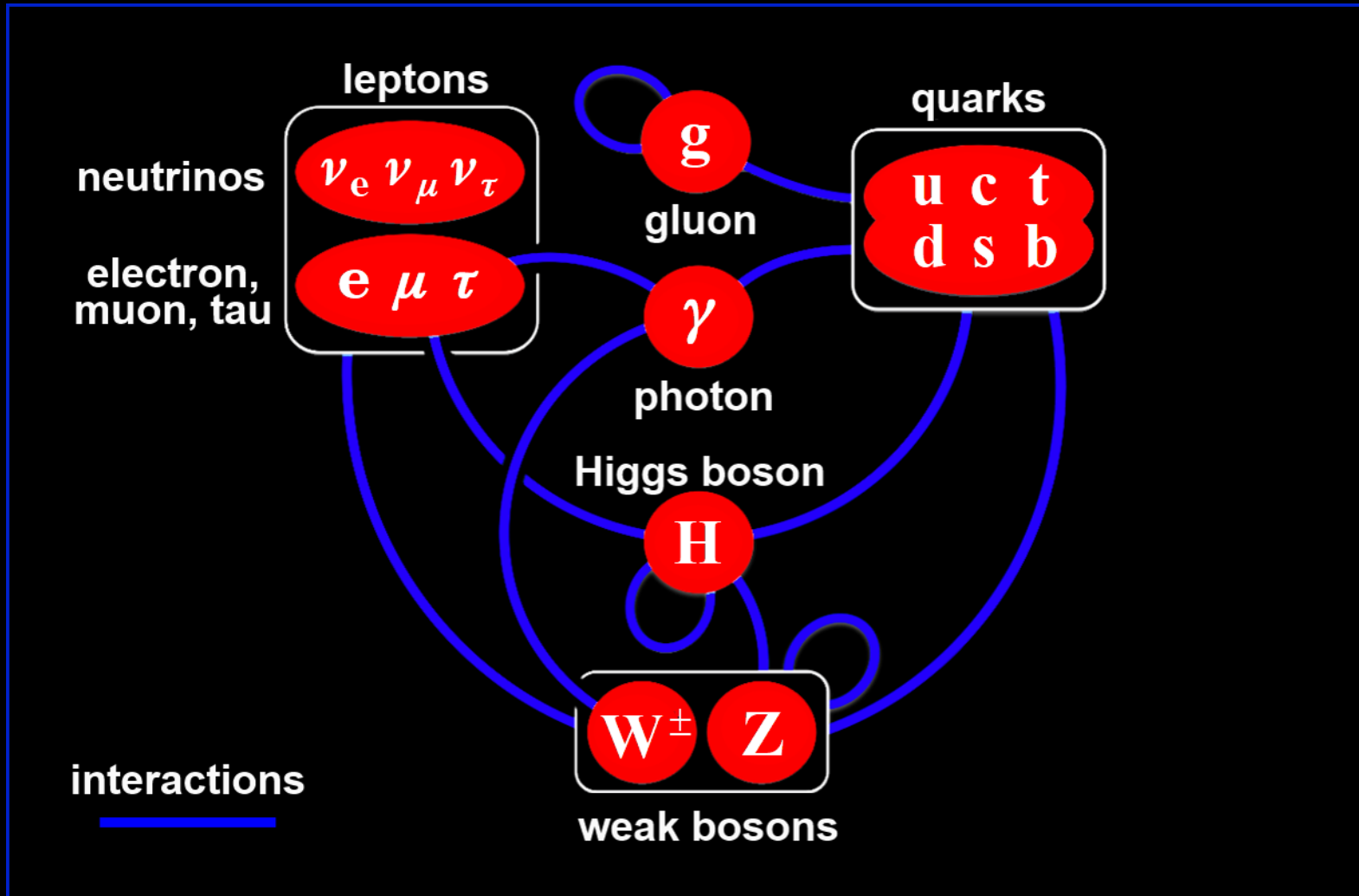
# Fundamental Bosons

---

- **Gluon – Carrier of strong force**
- **Photon – Carrier of electromagnetic force**
- **W and Z bosons – Mediators of weak force**
- **Higgs boson – Gives mass to W, Z & other particles via Higgs mechanism**

# Standard Model of Particle Physics

## Fundamental Particles and Interactions



Standard model is loose combination of two quantum field theories: electroweak theory and quantum chromodynamics. Image from Wikipedia "Standard Model" article (recolored)

# Standard Model of Particle Physics

## Action Principle Formulation in Lagrangian Density

Lagrangian density  $\mathcal{L} =$

$$\begin{aligned} & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}\text{tr}(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}\text{tr}(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) && \text{U(1), SU(2), SU(3) gauge terms} \\ & +(\bar{\nu}_L, \bar{e}_L)\tilde{\sigma}^\mu iD_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R\sigma^\mu iD_\mu e_R + \bar{\nu}_R\sigma^\mu iD_\mu \nu_R + \text{H.C.} && \text{lepton dynamical terms} \\ & -\frac{\sqrt{2}}{v} \left[ (\bar{\nu}_L, \bar{e}_L)\phi M^e e_R + \bar{e}_R\bar{M}^e\bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] && \text{electron, muon, tauon mass terms} \\ & -\frac{\sqrt{2}}{v} \left[ (-\bar{e}_L, \bar{\nu}_L)\phi^* M^\nu \nu_R + \bar{\nu}_R\bar{M}^\nu\phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right] && \text{neutrino mass terms} \\ & +(\bar{u}_L, \bar{d}_L)\tilde{\sigma}^\mu iD_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R\sigma^\mu iD_\mu u_R + \bar{d}_R\sigma^\mu iD_\mu d_R + \text{H.C.} && \text{quark dynamical terms} \\ & -\frac{\sqrt{2}}{v} \left[ (\bar{u}_L, \bar{d}_L)\phi M^d d_R + \bar{d}_R\bar{M}^d\bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix} \right] && \text{down, strange, bottom mass terms} \\ & -\frac{\sqrt{2}}{v} \left[ (-\bar{d}_L, \bar{u}_L)\phi^* M^u u_R + \bar{u}_R\bar{M}^u\phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix} \right] && \text{up, charmed, top mass terms} \\ & +\overline{(D_\mu\phi)}D^\mu\phi - m_h^2[\bar{\phi}\phi - v^2/2]^2/2v^2 && \text{Higgs dynamical and mass terms} \end{aligned}$$

Major achievement of mankind. From *An Introduction to the Standard Model of Particle Physics, 2nd Ed.* W.N. Cottingham and D.A. Greenwood, Cambridge University Press, Cambridge, 2007, Extracted by J.A. Shiflett, updated from PDG tables at [pdg.lbl.gov](http://pdg.lbl.gov), 2 Feb 2015. H.C.= Hermitian conjugate of prior terms

# Standard Model of Particle Physics

## Derivative Operations

---

$$D_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} = \left[ \partial_\mu - \frac{ig_1}{2} B_\mu + \frac{ig_2}{2} \mathbf{W}_\mu \right] \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \quad D_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \left[ \partial_\mu + \frac{ig_1}{6} B_\mu + \frac{ig_2}{2} \mathbf{W}_\mu + ig\mathbf{G}_\mu \right] \begin{pmatrix} u_L \\ d_L \end{pmatrix}$$

$$D_\mu \nu_R = \partial_\mu \nu_R, \quad D_\mu e_R = [\partial_\mu - ig_1 B_\mu] e_R \quad D_\mu u_R = \left[ \partial_\mu + \frac{i2g_1}{3} B_\mu + ig\mathbf{G}_\mu \right] u_R$$

$$D_\mu \phi = \left[ \partial_\mu + \frac{ig_1}{2} B_\mu + \frac{ig_2}{2} \mathbf{W}_\mu \right] \phi \quad D_\mu d_R = \left[ \partial_\mu - \frac{ig_1}{3} B_\mu + ig\mathbf{G}_\mu \right] d_R$$

---

# Action Principle Example

## – Classical EM Field

Lagrangian  
density



Maxwell  
Equations



# Action Principle Example – Classical EM Field

**Lagrangian density**  $\mathcal{L} = -\frac{1}{4\mu_0} F_{\mu\nu} F^{\mu\nu} + A_\nu J^\nu$

where  $F_{\mu\nu} = \nabla_\mu A_\nu - \nabla_\nu A_\mu = \partial_\mu A_\nu - \partial_\nu A_\mu =$  EM field 4-tensor,  $A_\nu =$  EM field 4-vector and  $J^\nu =$  4-current density

**Action**  $S[A_\mu] = \int \mathcal{L} \sqrt{-g} d^4x$

**Variation of action**  $\delta S = \int \left[ \frac{\partial(\sqrt{-g} \mathcal{L})}{\partial A_\beta} \delta A_\beta + \frac{\partial(\sqrt{-g} \mathcal{L})}{\partial(\partial_\alpha A_\beta)} \delta(\partial_\alpha A_\beta) \right] d^4x$

**Stationary action**  $\delta S = 0$  which can be shown to be satisfied by

**Heterogeneous Maxwell equations**  $-\nabla_\alpha F^{\alpha\beta} = \mu_0 J^\beta$

**Homogeneous Maxwell equations**  $\nabla_\alpha F^{*\alpha\beta} = 0$  ( follows from antisymmetry of  $F^{\alpha\beta}$  )

where  $F^{*\alpha\beta} =$  dual of  $F^{\alpha\beta}$

# Maxwell Equations

## Heterogeneous

---

$$-\nabla_{\alpha} F^{\alpha\beta} = \mu_0 J^{\beta} \left\{ \begin{array}{ll} \nabla \cdot \mathbf{E} = \rho_C / \epsilon_0 & \text{Gauss Law} \\ \nabla \times \mathbf{B} - \partial_t \mathbf{E} / c^2 = \mu_0 \mathbf{J}_C & \text{Extended Ampere law} \end{array} \right.$$

## Homogeneous

---

$$\nabla_{\alpha} F^{*\alpha\beta} = 0 \left\{ \begin{array}{ll} \nabla \cdot \mathbf{B} = 0 & \text{Gauss Law of Magnetism} \\ \nabla \times \mathbf{E} + \partial_t \mathbf{B} = \mathbf{0} & \text{Faraday Law} \end{array} \right.$$

In each pair of blue 3-vector equations the top one is the time component ( $\beta = 0$ ) and the bottom one is the space component

# Symmetry and Conservation

---

- Much of quantum field theory has to do with symmetries that exist in nature
- First examples deduced by Emmy Noether in 1915
- A number of others discovered since then
- Concept heavily exploited in standard model

# Symmetry and Conservation

## Lorentz Symmetry

Invariance	Conserved Quantity
Translation in time	Electric charge
Translation in space	Lepton generation number
Rotation in space	Hypercharge

## Discrete Symmetry

Invariance	Conserved Quantity
Coordinate inversion (P)	Spatial parity
Charge conjugation (C)	Charge parity
Time reversal (T)	Time parity
CPT	Product of parities

# Symmetry and Conservation

## Internal Symmetry

### Invariance

### Conserved Quantity

U(1) gauge transformation	Electric charge
U(1) gauge transformation	Lepton generation number
U(1) gauge transformation	Hypercharge
$U(1)_Y$ gauge transformation	Weak hypercharge
$U(2)$ [ $U(1) \times SU(2)$ ]	Electroweak force
SU(2) gauge transformation	Isospin
$SU(2)_L$ gauge transformation	Weak isospin
$P \times SU(2)$	G-parity
SU(3) "winding number"	Baryon number
SU(3) gauge transformation	Quark color
SU(3) (approximate)	Quark flavor
$S(U(2) \times U(3))$ [ $U(1) \times SU(2) \times SU(3)$ ]	Standard Model

From Wikipedia "Symmetry (physics)" article. An internal symmetry acts on the space of fields (i.e. space-time functions) and not on the space-time manifold

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Relativity of time interval

Relativity of length

Nonlinear speed addition

Relativity of simultaneity

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# Special Relativity

---

- Based in part on empirical observation that speed of light  $c$  is the same in all inertial frames
- More generally, takes the 4D spacetime interval as the fundamental kinematic invariant, whereby time, distance and simultaneity become relative
- Relativistic dynamics includes the famous  $E = mc^2$
- Spacetime foundation of quantum field theory and thereby of the standard model of particle physics

# Key Kinematic Phenomena of Special Relativity

## Twins Tale

- Nonaccelerated twin A observes, with instrumentation, his identical twin B moving at constant speed  $V$  relative to himself. A finds that B's clocks tick slower than his own by the factor  $1/\gamma$  and that B (and everything at rest around B) is foreshortened in the direction of motion by that same factor. B, with his instrumentation, draws the same conclusions about A and A's surroundings
- A's instrumentation, stationary in his rest frame, includes an array of synchronized clocks. B has similar equipment in his rest frame. A finds that B's clocks are out of synchronization in the direction of relative motion. B draws the same conclusion about A's clocks
- As A approaches B at speed  $V$  he fires a projectile at B (never really liked him anyway). The projectile travels at speed  $v$  relative to A's rest frame. No matter how close  $V$  and  $v$  are to  $c$ , the speed at which B perceives the projectile approaching is always less than  $c$
- B dodges the projectile, and avoids further assault by traveling to a distant star and back at a significant fraction of  $c$ . Still young upon his return, he is pleased to find that A has died of old age

$$1/\gamma = \sqrt{1 - (V/c)^2} \quad c = \text{speed of light}$$



# Key Kinematic Phenomena of Special Relativity

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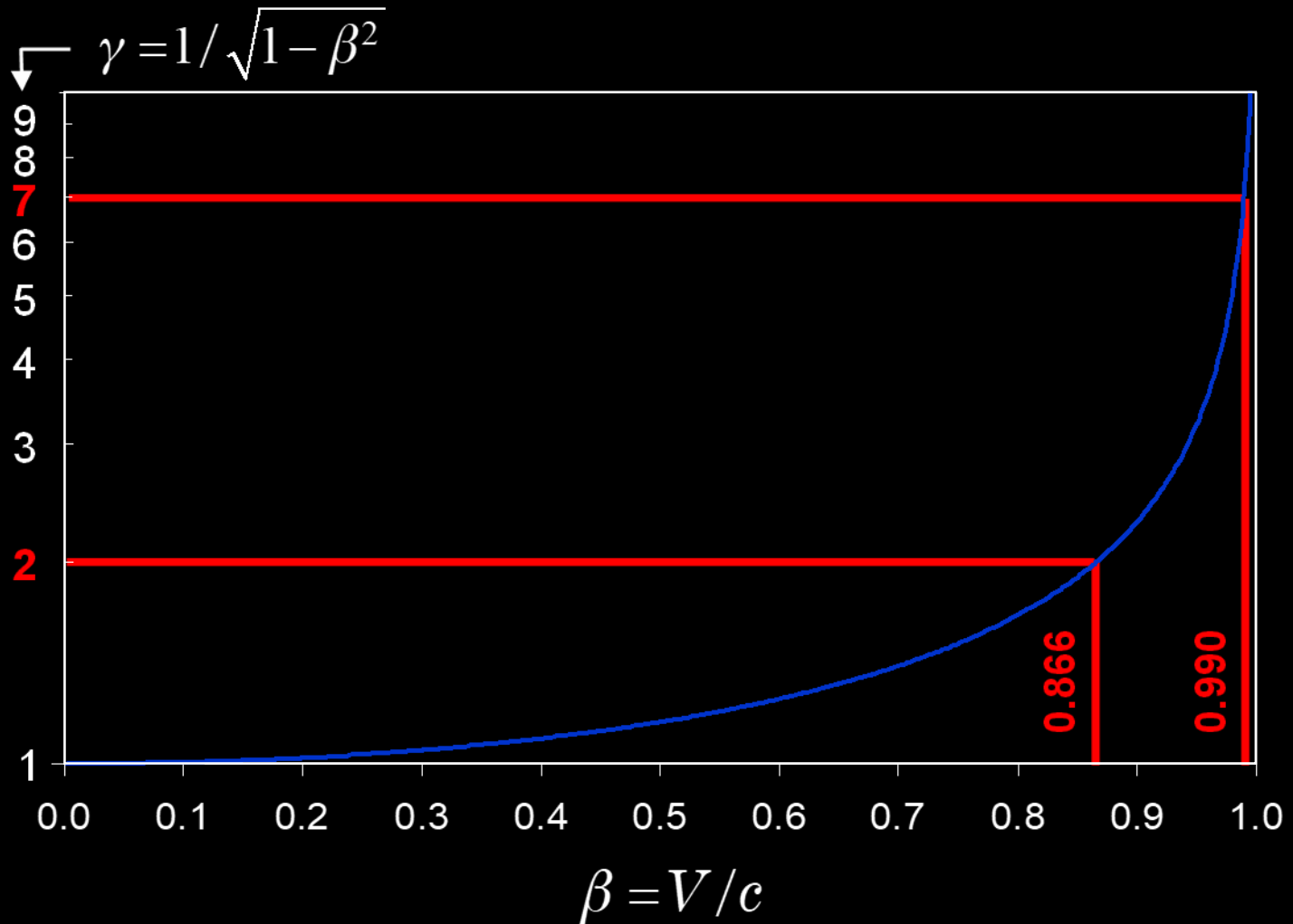
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# Stretch Factor



# Relativistic Kinematics in Direction of Motion

Based on Invariance of  $\Delta \mathbf{x} \cdot \Delta \mathbf{x}$

$$\bar{t}_2 - \bar{t}_1 = (t_2 - t_1)/\gamma$$

Relativity of time interval

$$\bar{L} = L/\gamma$$

Relativity of length

$$\bar{v} = \frac{V + v}{1 + Vv/c^2}$$

Non-linear speed addition

$$\bar{t}_2 - \bar{t}_1 = -\gamma V (x_2 - x_1)/c^2$$

Relativity of simultaneity\*

$\Delta \mathbf{x}$  = 4D displacement vector.  $c$  = light speed (invariant among inertial frames).  $V$  = relative speed of frames.

\*Assumes events of interest are simultaneous in unbarred frame (last equation only)

# Relativistic Kinematics in Direction of Motion

Based on Invariance of  $\Delta \mathbf{x} \cdot \Delta \mathbf{x}$

$$t_2 - t_1 = (\bar{t}_2 - \bar{t}_1) / \gamma$$

Relativity of time interval

$$L = \bar{L} / \gamma$$

Relativity of length

$$v = \frac{V + \bar{v}}{1 + V \bar{v} / c^2}$$

Non-linear speed addition

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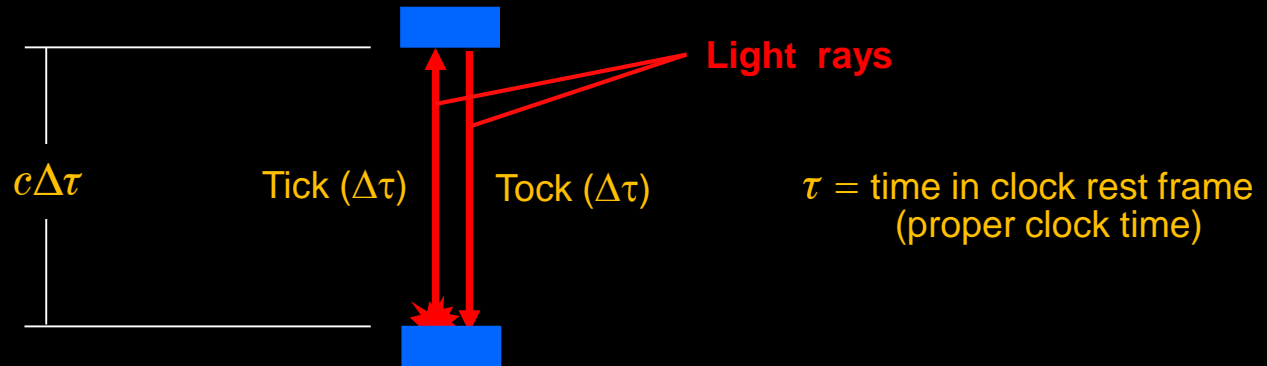
First and second laws

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# Relativity of Time Interval – Derivation

Based on invariance of light speed across inertial frames

Two ticks of light clock in clock rest frame

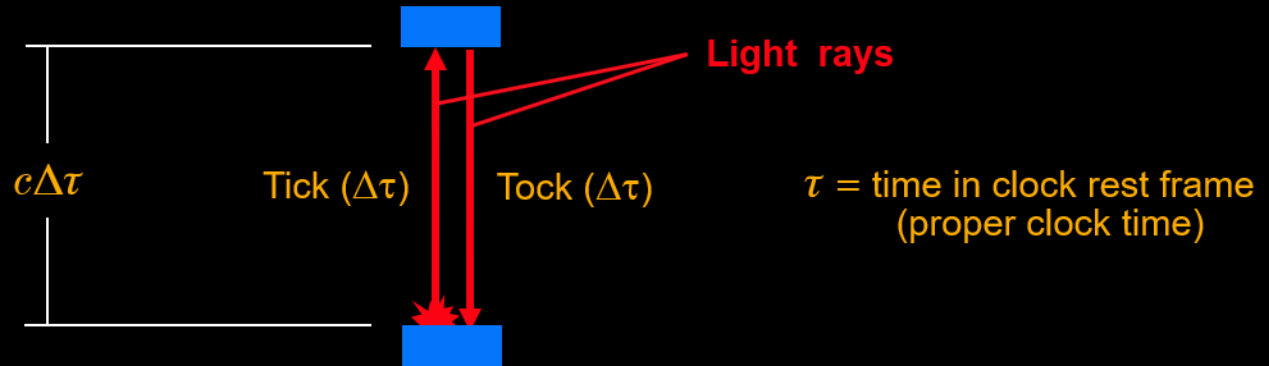




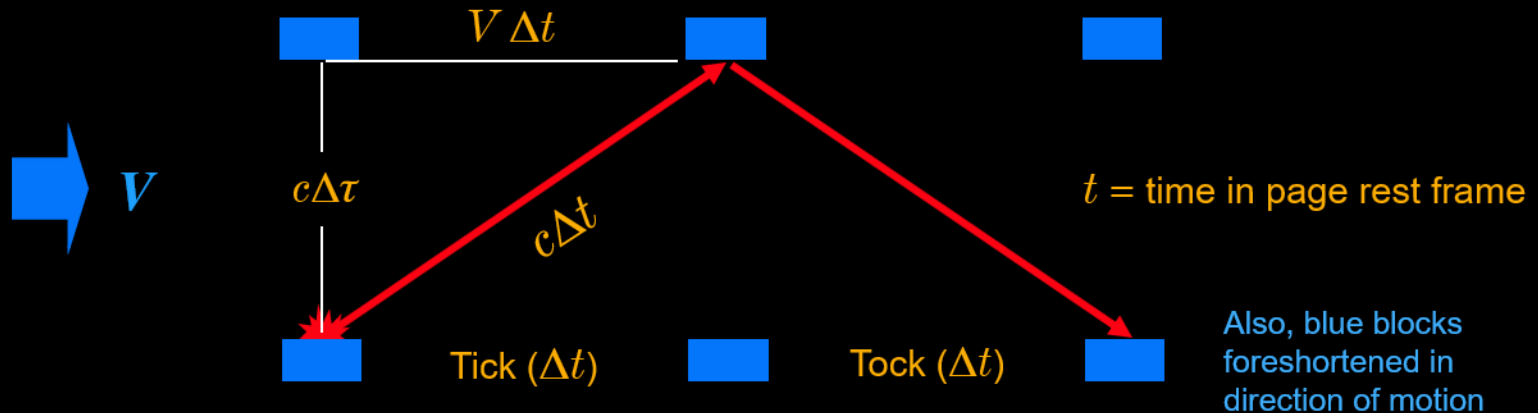
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Based on invariance of light speed across inertial frames

Two ticks of light clock in clock rest frame



Two ticks of light clock moving rightward at speed  $V$  in slide rest frame



Pythagorean theorem  $(c\Delta t)^2 = (c\Delta\tau)^2 + (V\Delta t)^2 \Rightarrow \Delta\tau = \Delta t/\gamma$

# Situations Where Relativity of Time of Practical Importance

---

- The slowing of time at high speeds is significant in each particle collision in the Large Hadron Collider. Particles are brought together at near-light speeds. Highly unstable particles created in collisions also travel at high speeds – high enough to survive long enough to be detected in frame of experiment
- The GPS system provides another example. Speeds of the GPS satellites are not particularly high, but the time-keeping precision needed for accurate results requires that both special and general relativistic effects be accounted for

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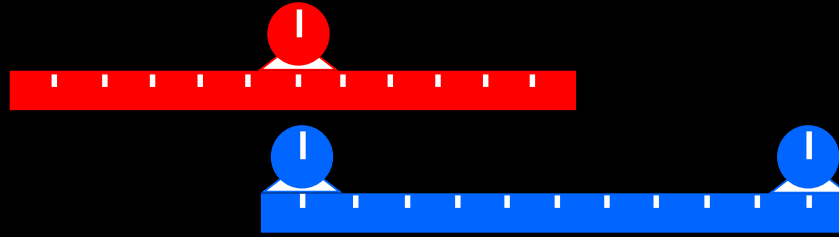
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# Relativity of Length (and Time Interval)

Size Foreshortened (and Time Slowed) in Direction of Motion

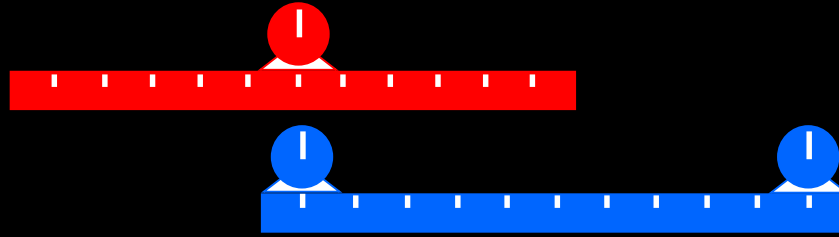
Synchronized clocks and ruled platforms in shared inertial rest frame



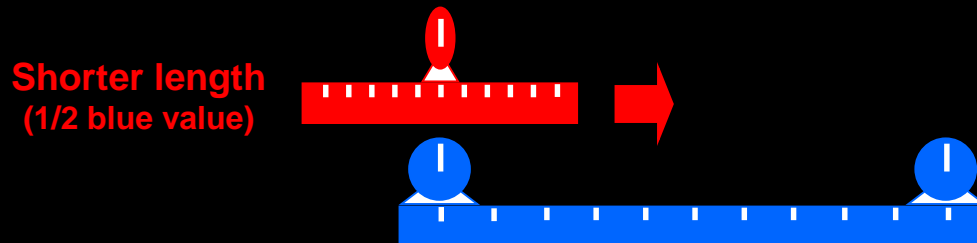
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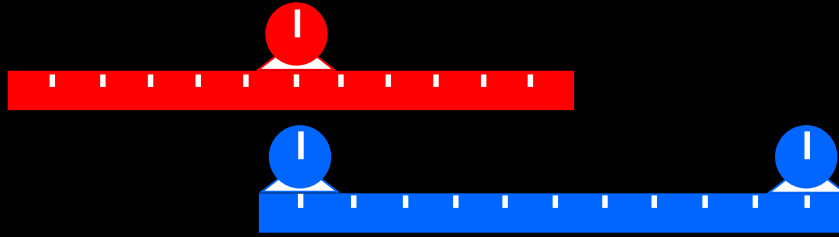
Red system moves rightward at high speed ( $0.866c \Rightarrow \gamma = 2$ )



# Relativity of Length (and Time Interval)

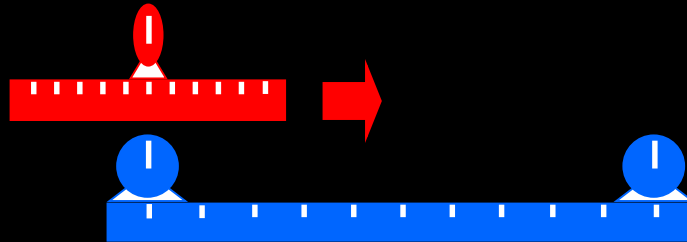
Size Foreshortened (and Time Slowed) in Direction of Motion

Synchronized clocks and ruled platforms in shared inertial rest frame



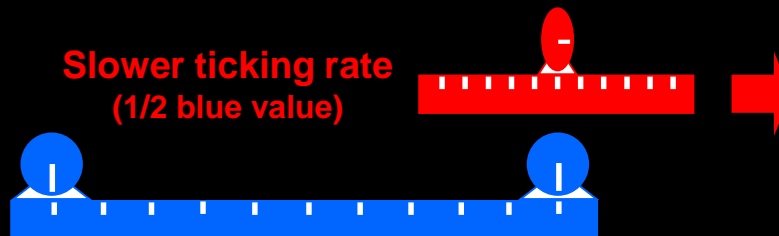
Red system moves rightward at high speed ( $0.866c \Rightarrow \gamma = 2$ )

Shorter length  
(1/2 blue value)



One-half revolution of blue clock hands later

Slower ticking rate  
(1/2 blue value)



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Gravitoelectromagnetism

Gravitational waves

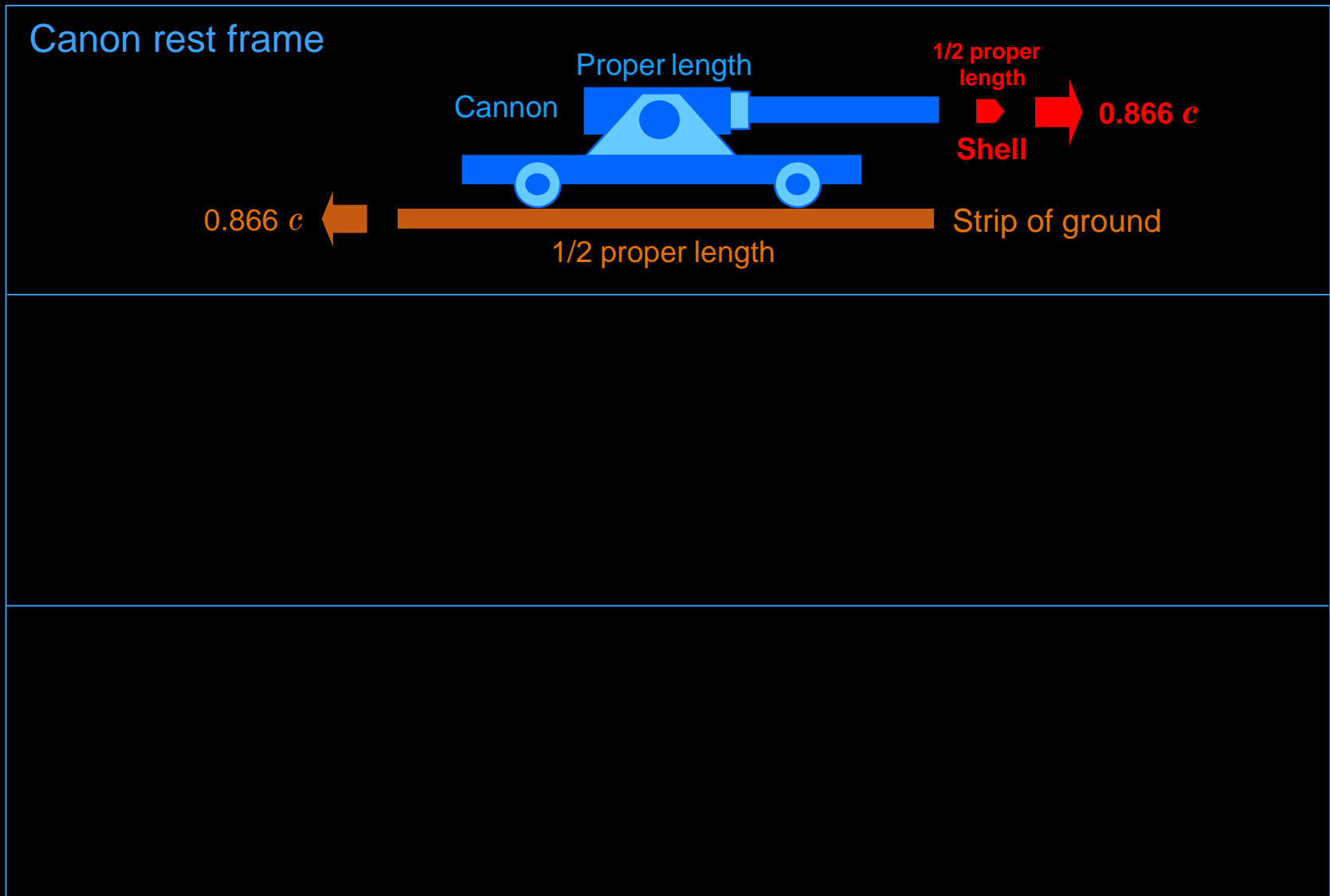
## Thermodynamics

First and second laws

Entropy generation

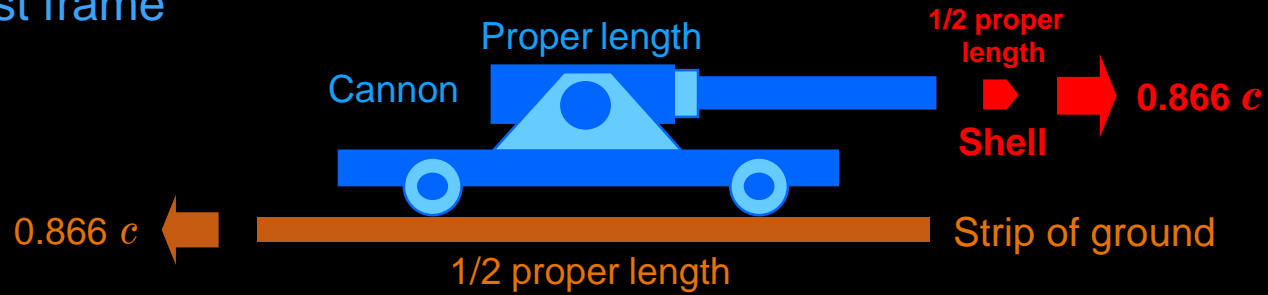


# Non-Linear Speed Addition

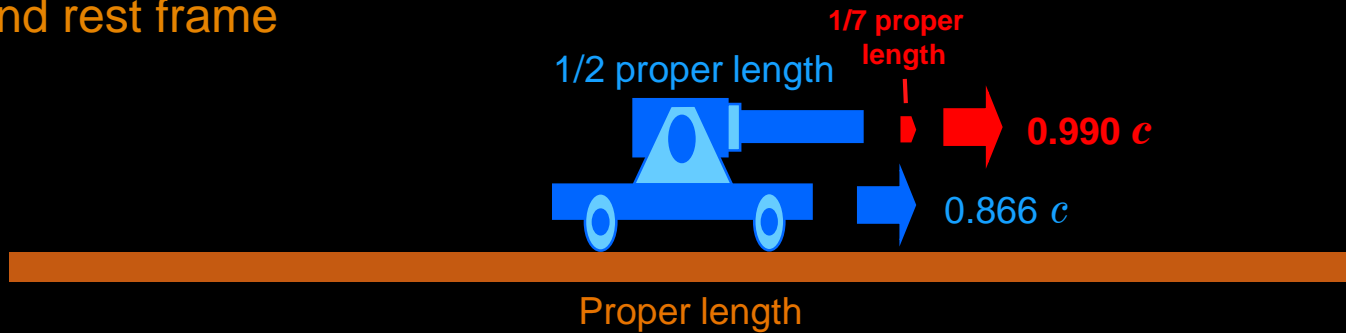


# Non-Linear Speed Addition

Canon rest frame

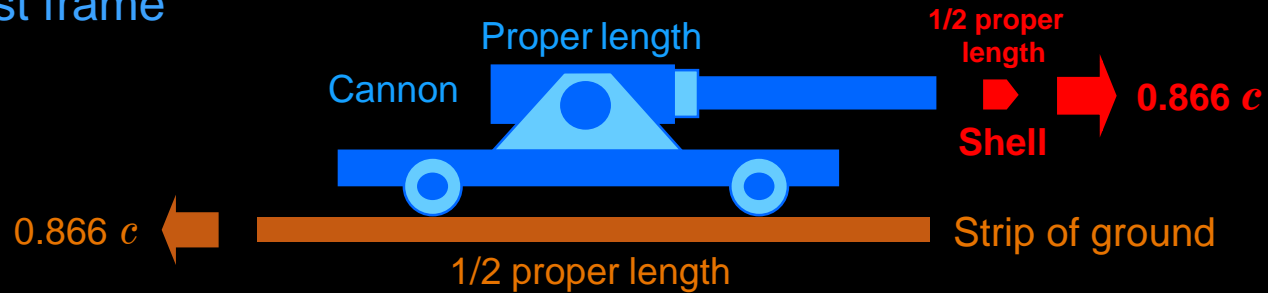


Ground rest frame

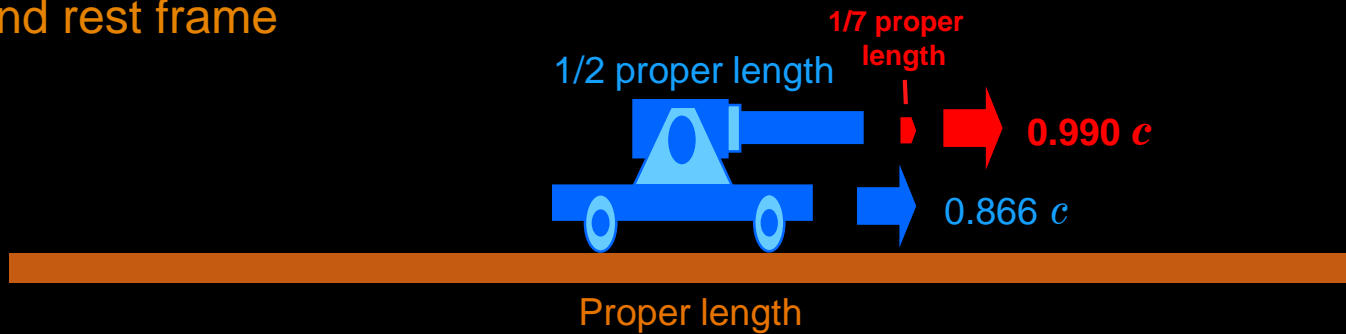


# Non-Linear Speed Addition

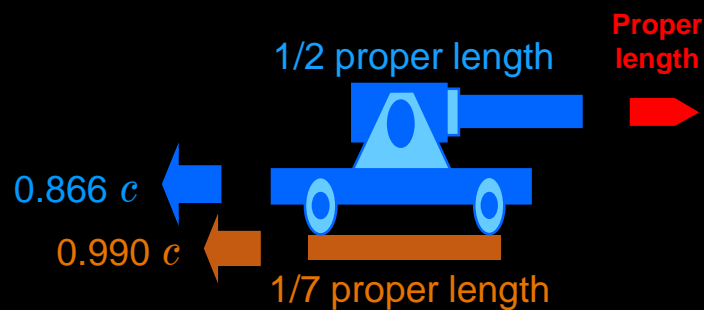
Canon rest frame



Ground rest frame



Shell rest frame



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# Different Event Orderings for Different Observers

---

- Recall from above that spatially separated events which occur simultaneously in one frame cannot occur simultaneously in a second frame moving parallel to the direction of separation
- As a consequence, multiple events can occur in different sequences in different frames

# Different Event Orderings in Twin Paradox Problem

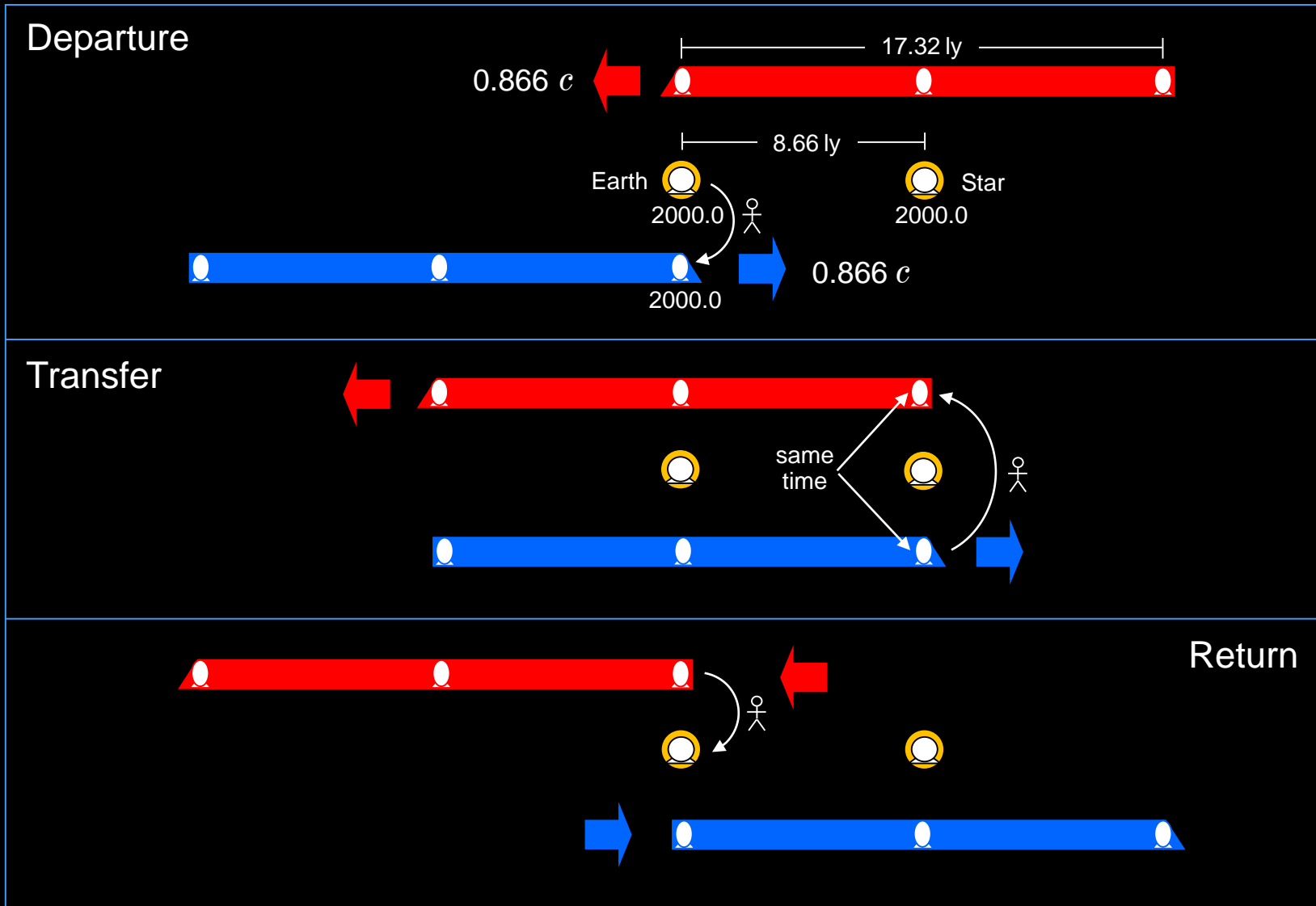
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- The twin paradox problem can provide examples of event orderings that differ from one frame to another
- One of two Earth-born twins travels to a distant star and back by hitching rides on outbound and inbound astrotrains\*
- Consider the trip in each of three reference frames: (1) Earth-star (2) outbound train (3) inbound train

\*Such fanciful trains also can be found in *Spacetime Physics* (1992) by Taylor and Wheeler

# Twin Paradox

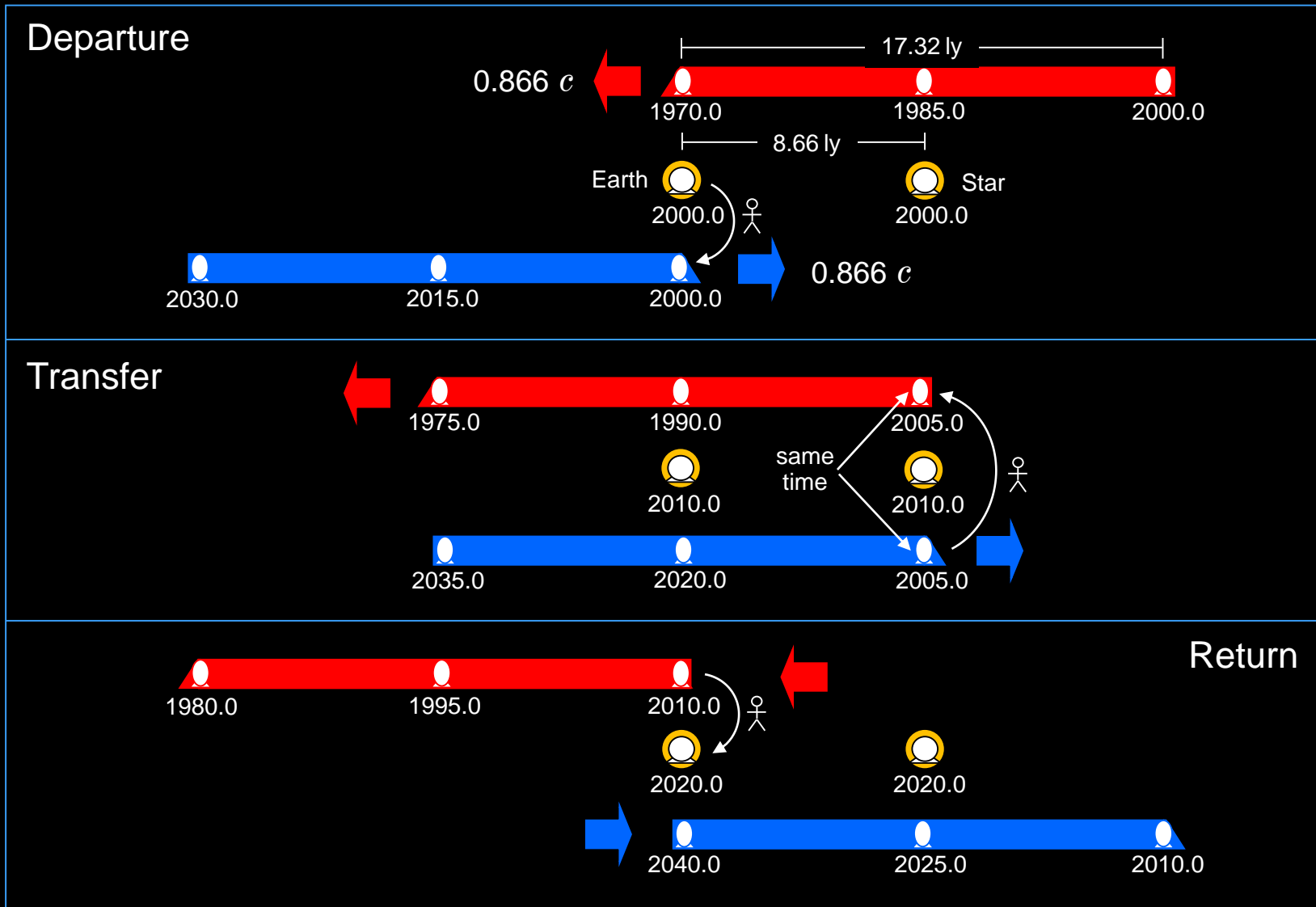
## Trip in Earth-Star Rest Frame: Givens



Note that Earth and star clock faces are circular but train clock faces are foreshortened in direction of motion

# Twin Paradox

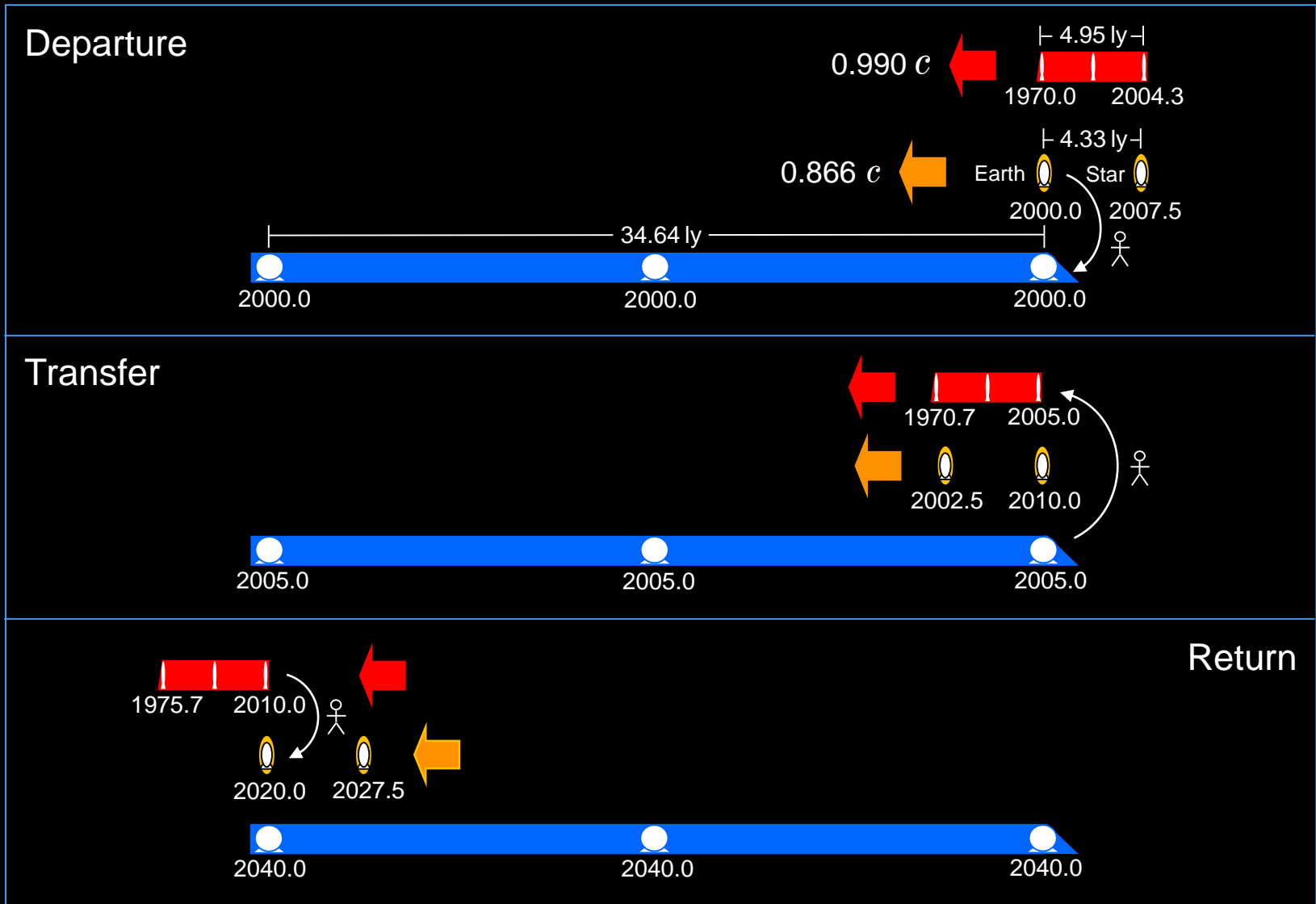
Trip in Earth-Star Rest Frame: All Clock Times





# Twin Paradox

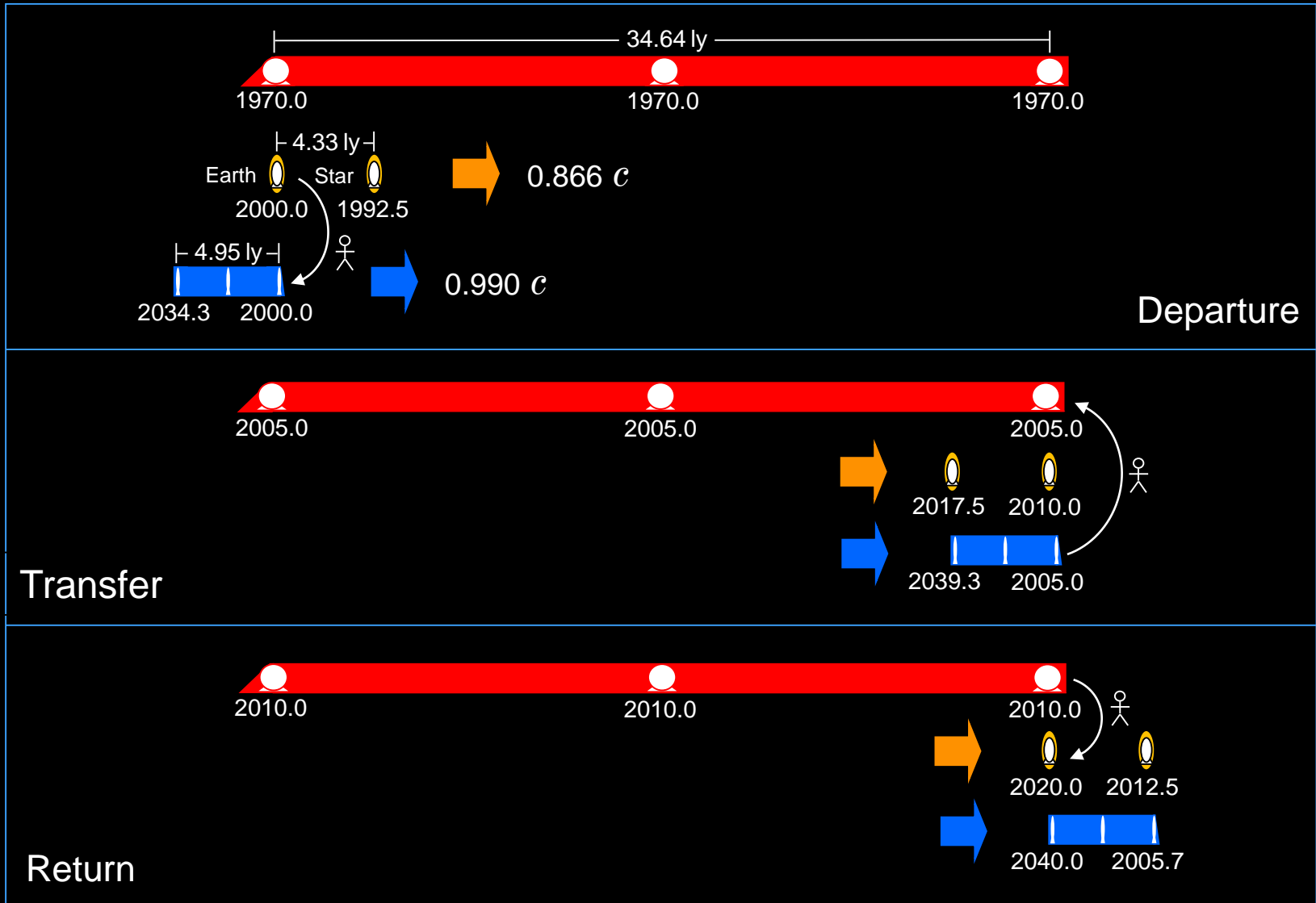
## Trip in Outbound Train Rest Frame



Outbound train at true length. Severe foreshortening of inbound train (including clock faces)

# Twin Paradox

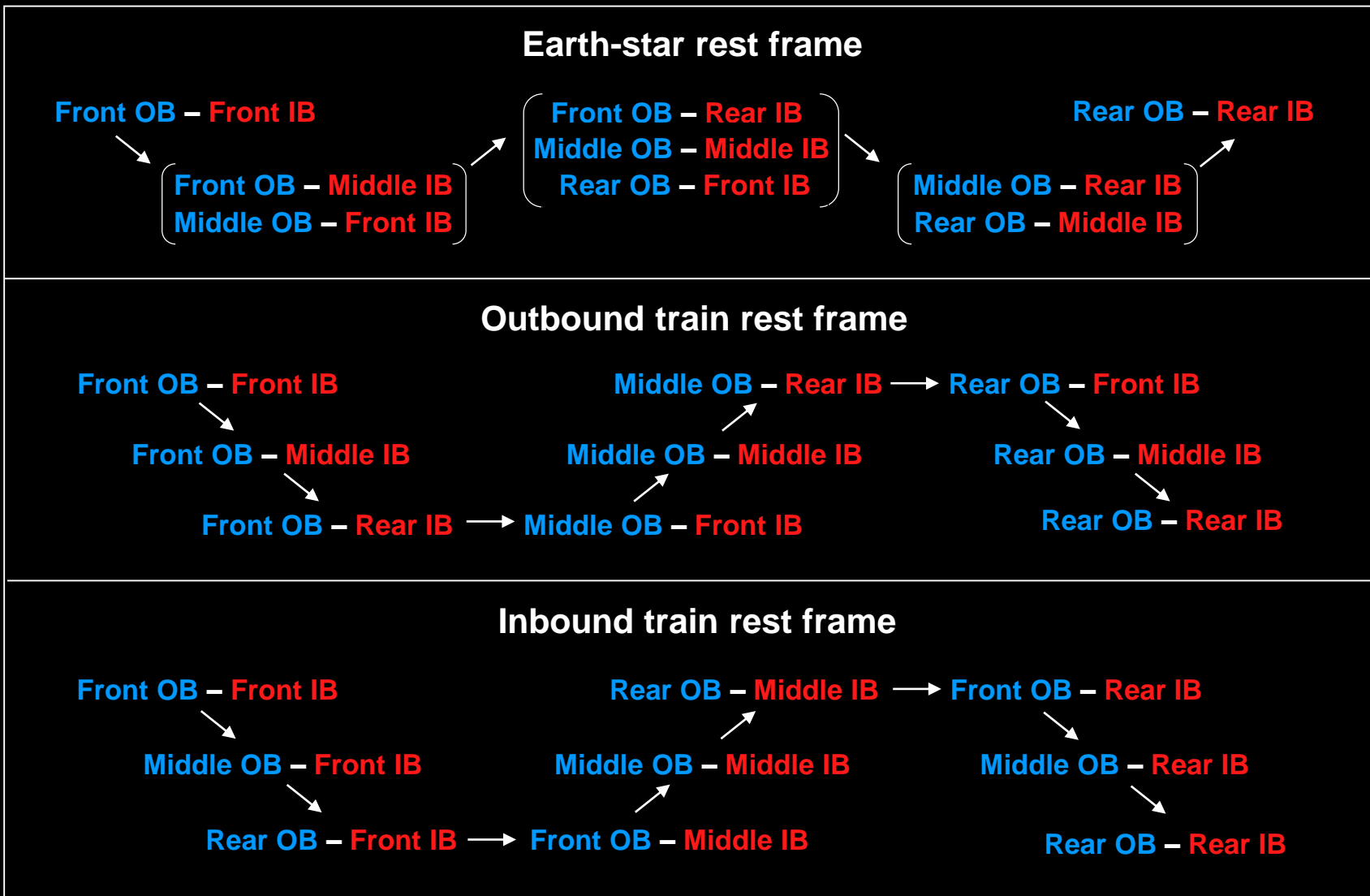
## Trip in Inbound Train Rest Frame



Inbound train at true length. Severe foreshortening of outbound train (including clock faces)

# Twin Paradox

## Frame-Dependent Ordering of Train Clock Passings



Bracketed events are simultaneous. No passings are simultaneous in either train rest frame

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# Special Relativistic Dynamics

4-Momentum & Components, Including Mass-Equivalent Energy

$$\mathbf{p} = m\mathbf{u}$$

$$\mathbf{u} = d\mathbf{x}/d\tau \quad d\mathbf{x} = \boldsymbol{\eta}_0 c dt + d\mathbf{x} \quad dt = \gamma d\tau \quad d\mathbf{x} = \mathbf{v} dt$$



$$\mathbf{p} = \boldsymbol{\eta}_0 \gamma m c + \gamma m \mathbf{v} = \boldsymbol{\eta}_0 p^0 + \mathbf{p}$$



$$p^\mu = (p^0, \mathbf{p}) = (E/c, \mathbf{p})$$

$$E = p^0 c = \gamma m c^2 = E' + K$$

$$E' = m c^2 \quad K = (\gamma - 1) m c^2 = \frac{1}{2} m v^2 \left( 1 + \frac{3}{4} \beta^2 + \frac{5}{8} \beta^4 + \dots \right)$$

$\mathbf{p}$  = 4-momentum,  $m$  = mass,  $\mathbf{u}$  = 4-velocity,  $d\mathbf{x}$  = 4-displacement,  $d\tau$  = proper time interval,  $\boldsymbol{\eta}_0$  = temporal base vector,  $c$  = speed of light,  $dt$  = inertial time interval,  $d\mathbf{x}$  = displacement (orthogonal to  $\boldsymbol{\eta}_0$ ),  $\gamma$  = stretch factor,  $\mathbf{v}$  = velocity,  $\mathbf{p}$  = momentum,  $p^0$  = 4-momentum time component,  $p^\mu$  = 4-momentum components,  $E$  = energy,  $E'$  = rest (mass-equivalent) energy,  $K$  = relativistic kinetic energy,  $\beta = v/c$

# Special Relativistic Dynamics

## Single Particle Equation of Motion & Components

4-vector (invariant) equation of motion

$$\mathbf{a} = \hat{\mathbf{K}}$$

$v \ll c$

$v < c$

3-vector low-speed equations

3-vector high-speed equations

$$\mathbf{a} = \hat{\mathbf{F}}$$

$$d\frac{1}{2}v^2 = \hat{\mathbf{F}} \cdot d\mathbf{x}$$

space  
component

time  
component

$$\mathbf{a} = (\mathbf{1} - \beta\beta) \cdot \hat{\mathbf{F}} / \gamma$$

$$d\hat{K} = \hat{\mathbf{F}} \cdot d\mathbf{x}$$

$\mathbf{a}$  = 4-acceleration,  $\hat{\mathbf{K}}$  = 4-force per unit mass,  $v$  = speed,  $c$  = light speed,  $\mathbf{a}$  = acceleration,  $\hat{\mathbf{F}}$  = force per unit mass,  $d\mathbf{x}$  = displacement,  $\mathbf{1}$  = identity tensor,  $\beta = \mathbf{v}/c$ ,  $\gamma = 1/\sqrt{1-\beta^2}$ ,  $\beta = v/c$ ,  $\hat{K} = (\gamma - 1)c^2 = \frac{1}{2}v^2 \left(1 + \frac{3}{4}\beta^2 + \frac{5}{8}\beta^4 + \dots\right)$  = relativistic KE per unit mass

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\*Cosmological applications covered in Big Picture Science presentation on Observable Universe

# General Relativity

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- Treats gravity as local curvature of spacetime, said curvature caused by presence of energy and/or momentum
- Successful predictions include slower clock rates in stronger gravitational fields, black holes, gravito-electromagnetism and gravity waves, among others
- Underlying theory of Big Bang Cosmology in form of  $\Lambda$ CDM model\*

\* $\Lambda$  = Einstein cosmological constant. CDM = Cold Dark Matter



# General Relativity

*Spacetime tells matter how to move; matter tells spacetime how to curve*

– John Archibald Wheeler

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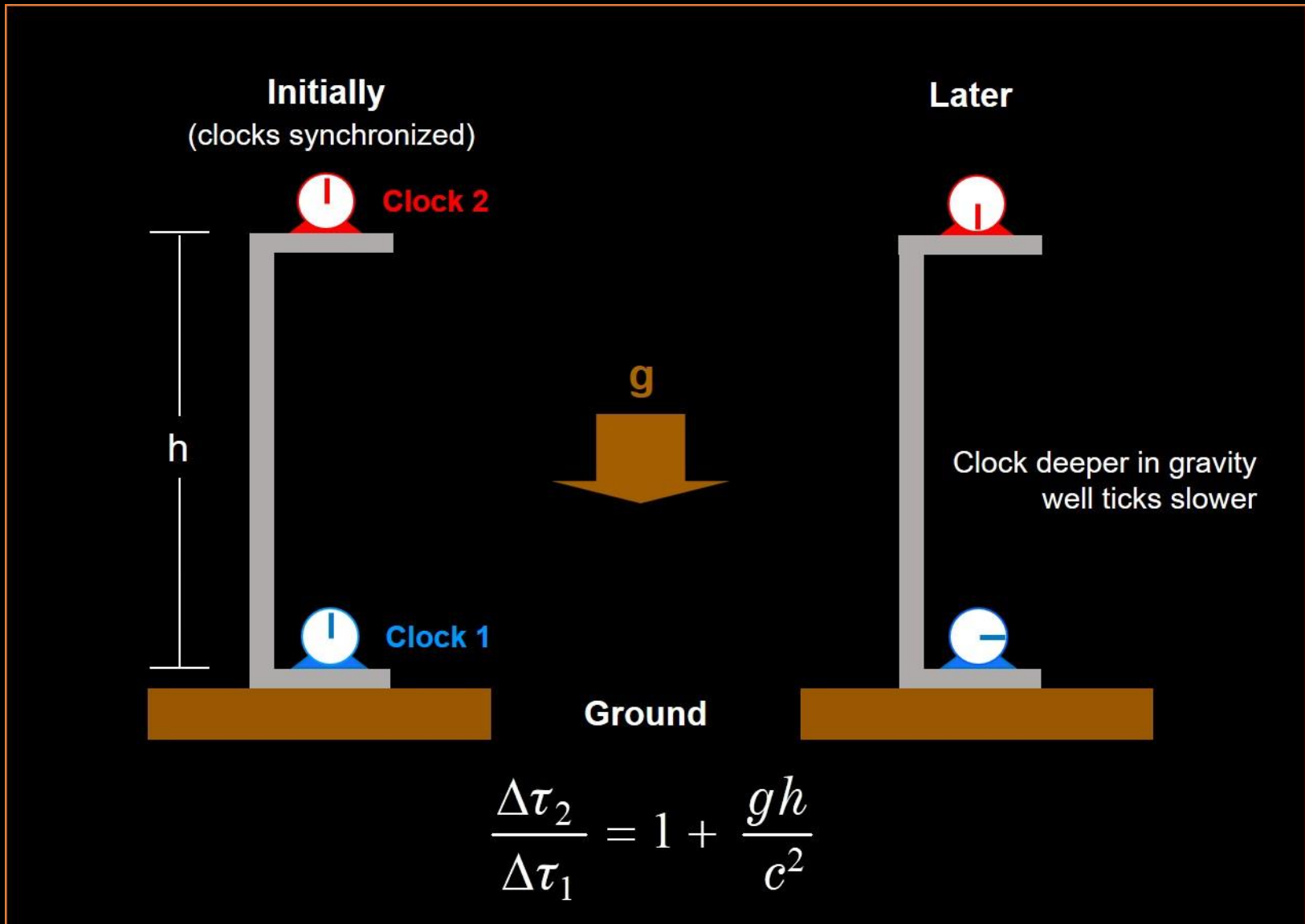
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# Slowing of Time by Gravity

Weak Gravitational Field (e.g., that of Earth)



First experimental confirmation of effect: Pound, R. V.; Rebka Jr. G. A. (November 1, 1959). "Gravitational Red-Shift in Nuclear Resonance". *Physical Review Letters*. 3 (9): 439–441

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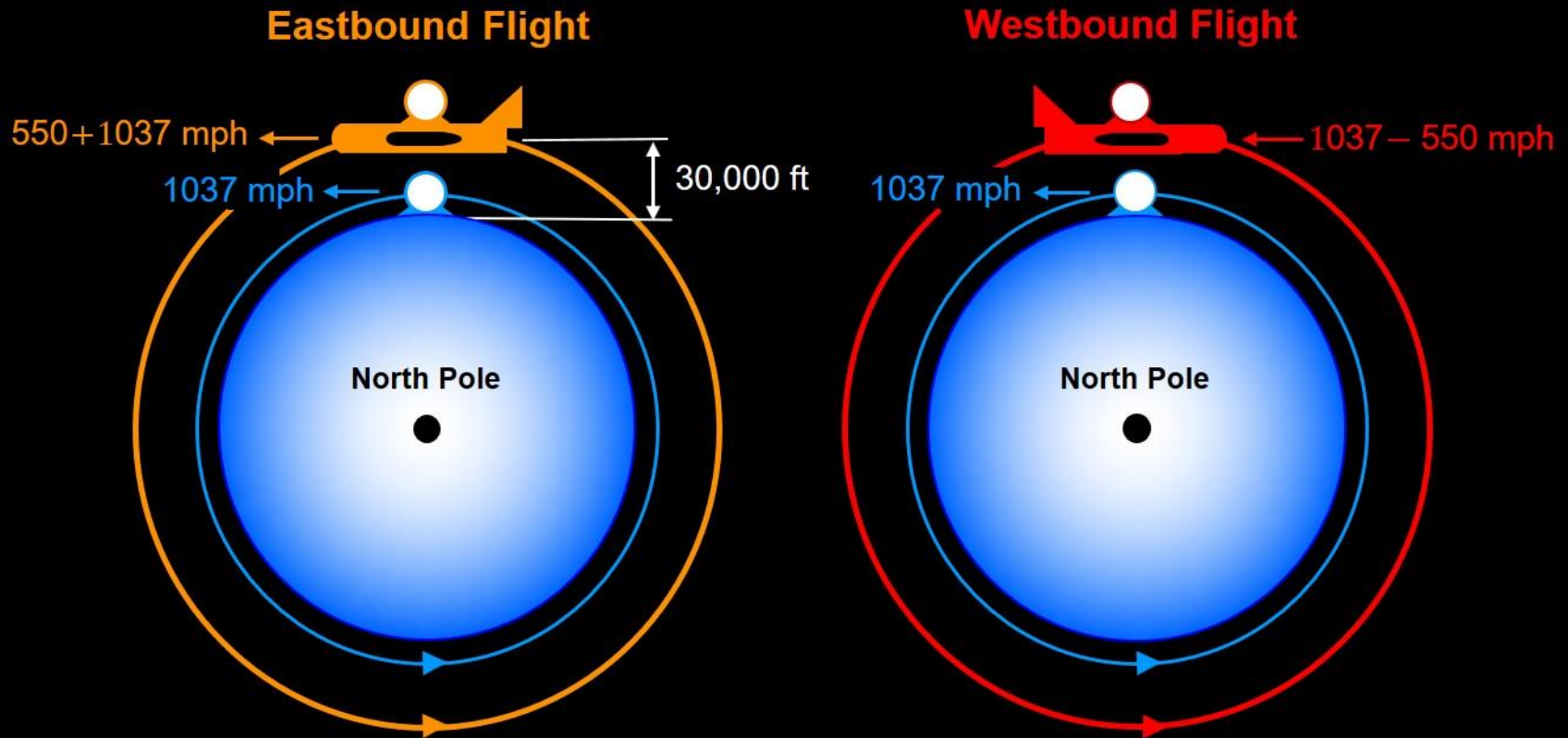
# Hafele-Keating Experiment

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- Demonstrates impact of special and general relativistic effects on ticking rates of clocks flown around the world in east-bound and west-bound directions
- First version carried out in 1971 by Hafele and Keating.\* Repeated multiple times with increasing precision
- Effects involved have implications for the GPS system
- Only idealized version of the experiment considered here

\*Hafele, J. C.; Keating, R. E. (July 14, 1972). "Around-the-World Atomic Clocks: Predicted Relativistic Time Gains". *Science*. 177 (4044): 166–168

# Idealized Hafele-Keating Experiment



Two clocks are flown around the equator – one eastward, one westward. A third clock sits on the equator. Which of the three clocks ticks fastest and which ticks slowest? Evaluate in a nonrotating reference frame with origin at the center of the Earth

# Idealized Hafele-Keating Experiment

## Qualitative Analysis

- **General relativistic effect** Gravity slows time. Both flying clocks therefore gain time on the ground clock (GC), which, at a lower elevation, experiences a stronger gravitational field
- **Special relativistic effect** Motion slows time. The slowest moving, west-bound flying clock (WBFC) therefore gains time on both the GC and the eastbound flying clock (EBFC)
- **Net effect** The WBFC clearly ticks fastest, as it gains time on both of the other clocks. Which clock ticks slowest cannot be determined from qualitative analysis

## Quantitative Analysis

- Quantitative analysis (or an actual experiment) will reveal that the EBFC loses more time to the GC from its higher speed than it gains from its higher elevation. The EBFC therefore ticks the slowest of the three clocks, with the parameter values of this particular problem

The net times gained and lost here involve tens of nanoseconds. Such relativistic effects must be accounted for in the GPS system, otherwise the system would quickly become useless as a navigational aid

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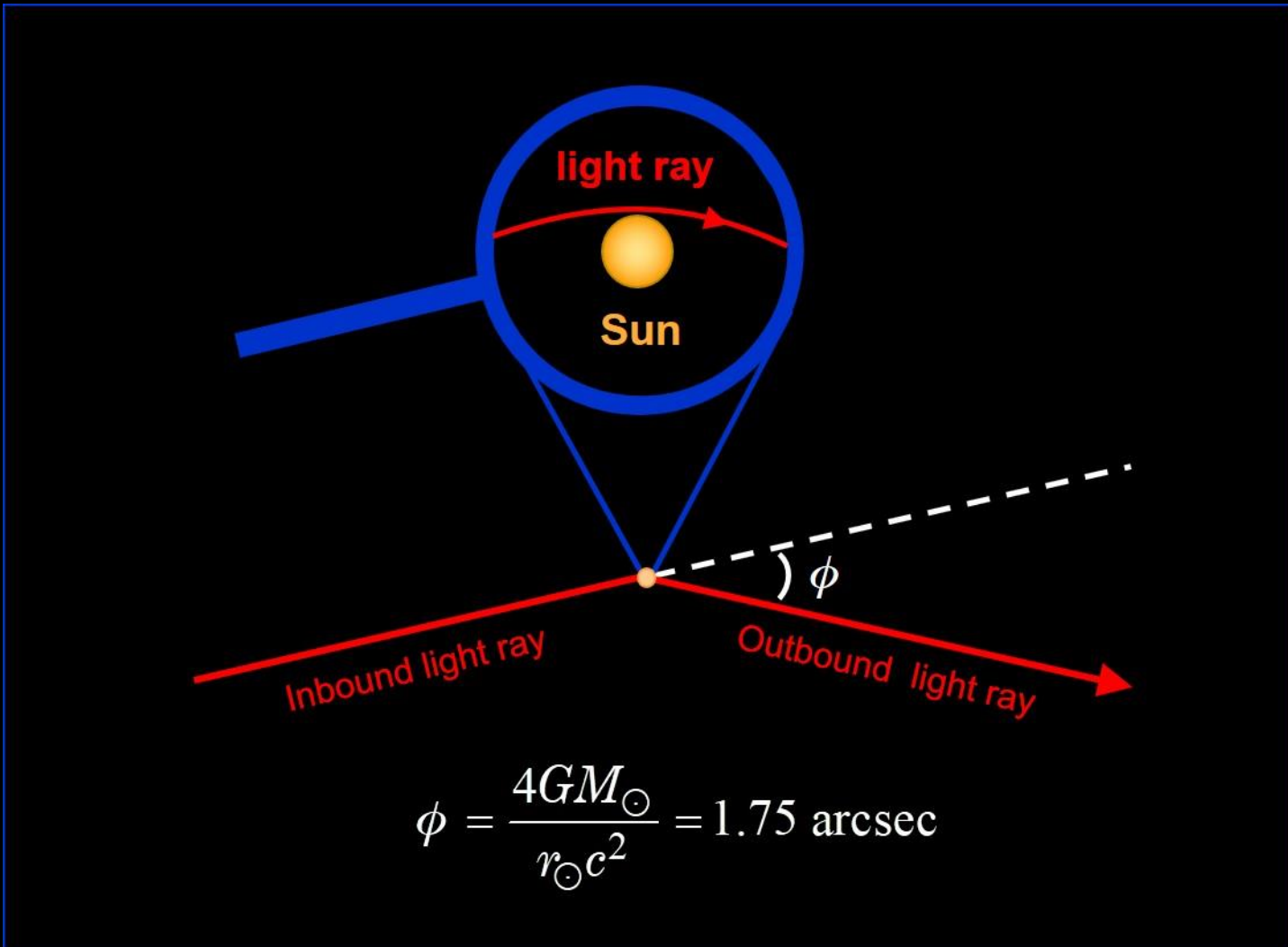
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Entropy generation



# Bending of Light by Gravity



Bending exaggerated in image. Confirmation of above phenomena during a solar eclipse [Eddington et al (1919)] brought Einstein's general theory to attention of general public

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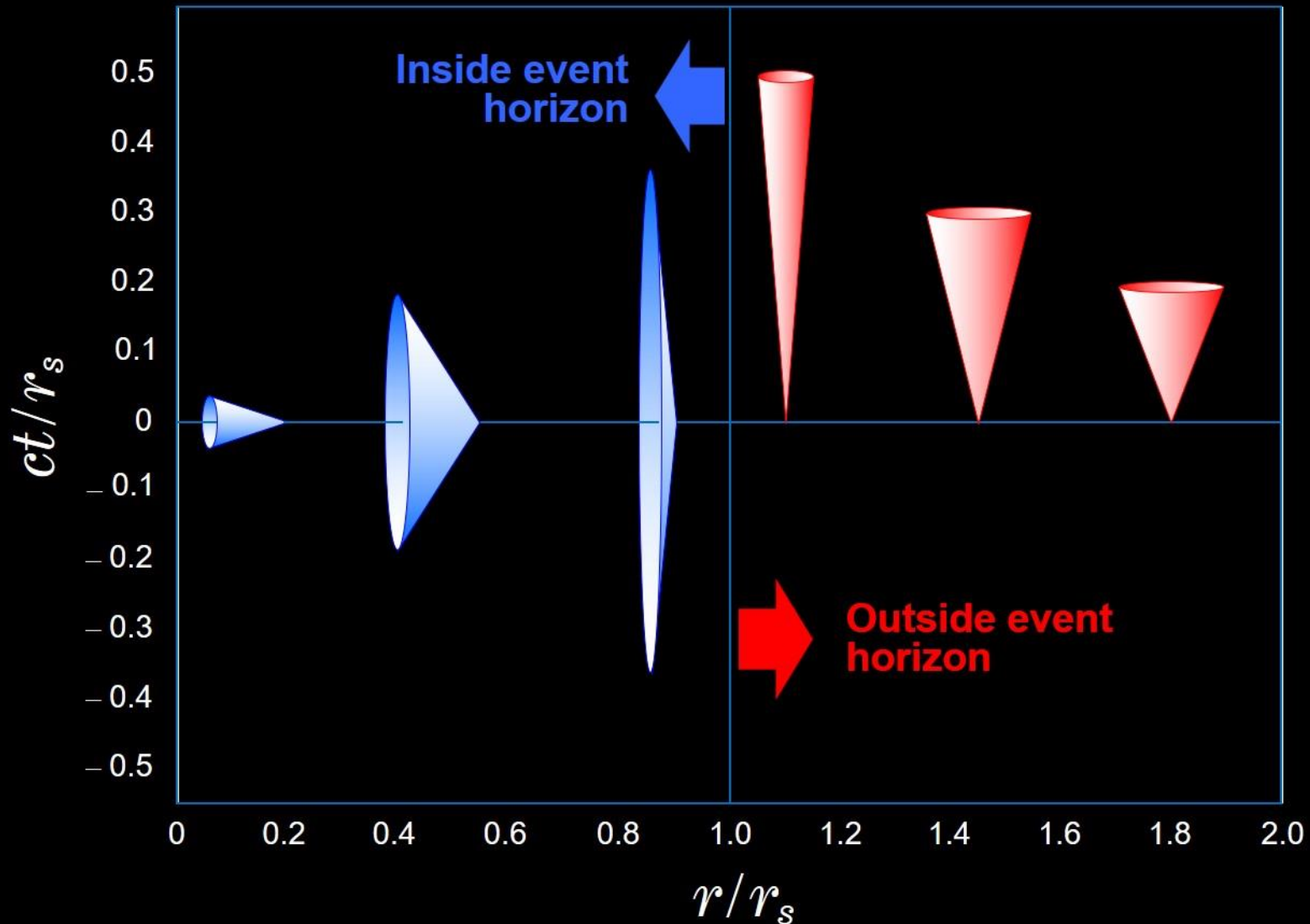
Entropy generation

# Black Holes

---

- Remnants of supermassive stars, so dense and massive that even light cannot escape once inside the bounding event horizon
- Once formed, black holes can continue to grow by absorbing more nearby matter
- Such absorption has led to the presence of supermassive black holes at the centers of most galaxies, where matter is concentrated

# Trapping of Light in Black Hole



$r_s = 2MG/c^2$  is the Schwarzschild radius (also event horizon for a black hole). Coordinates  $r$  and  $t$  swap signs inside event horizon. Once inside the event horizon light cannot escape

# Black Holes

---

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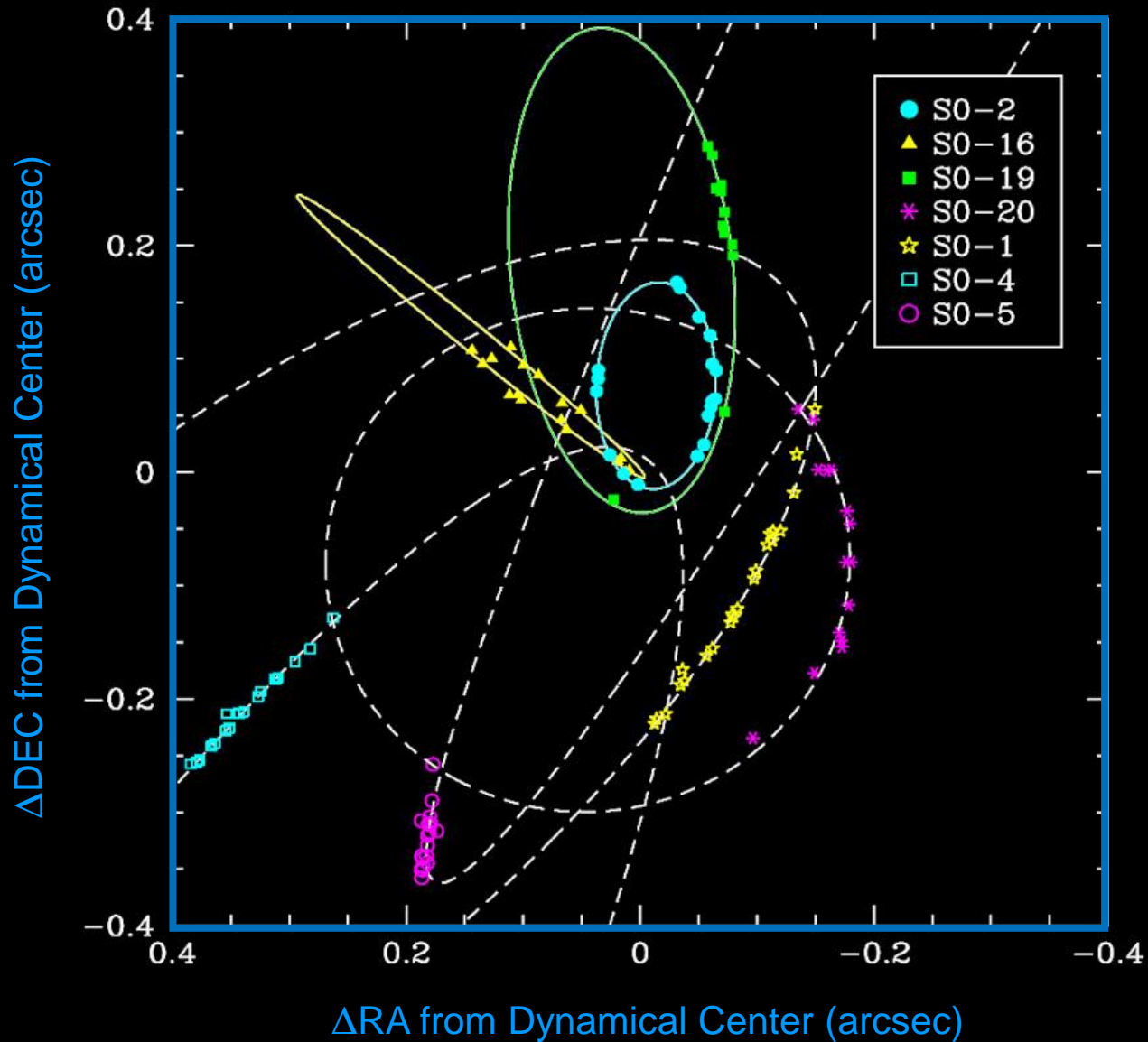
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# Sagittarius A\*

Supermassive Black Hole at Milky Way Center



Stars orbiting unseen Sagittarius A\*. Mass roughly 4 million times that of Sun. Ghez et al (2004)], "Stellar Orbits Around the Galactic Center Black Hole", 620:744–757, 2005 February 20, *Astrophysical Journal*

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# Gravitoelectromagnetism

---

- Under weak-field, slow-motion conditions, the central equation of general relativity, the Einstein field equation, yields four partial differential equations mathematically equivalent to the Maxwell equations of electromagnetism
- Predictions extracted from these gravitoelectromagnetic equations are claimed to agree with data collected by an orbiting satellite

# Electromagnetism and Gravitoelectromagnetism

## Analogous Field Equations

### 4D EM Field Equation

### 4D Gravitational Field Eqn

$$-\nabla \cdot \mathbf{F} = \mu_0 \mathbf{J}_C$$

$$\mathbf{G} = \kappa \mathbf{T}$$

### Maxwell Equations

### GEM Equations

$$\nabla \cdot \mathbf{E} = \rho_C / \epsilon_0$$

$$\nabla \cdot \mathbf{g} = \rho / \alpha$$

$$\nabla \times \mathbf{B} - \partial_t \mathbf{E} / c^2 = \mathbf{J}_C / (\epsilon_0 c^2)$$

$$\nabla \times \frac{1}{2} \mathbf{h} - \partial_t \mathbf{g} / c = \mathbf{J}_M / (\alpha c)$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \cdot \mathbf{h} = 0$$

$$\nabla \times \mathbf{E} + \partial_t \mathbf{B} = \mathbf{0}$$

$$\nabla \times \mathbf{g} + \partial_t \frac{1}{2} \mathbf{h} / c = \mathbf{0}$$

The invariant electromagnetic and gravitational field equations are written in 4-vectors and 4-tensors. The Maxwell (electromagnetic) and GEM (gravitoelectromagnetic) equations are written in 3-vectors. The GEM equations come from the linearized (weak-field) form of the Einstein field equation  $\mathbf{G} = \kappa \mathbf{T}$

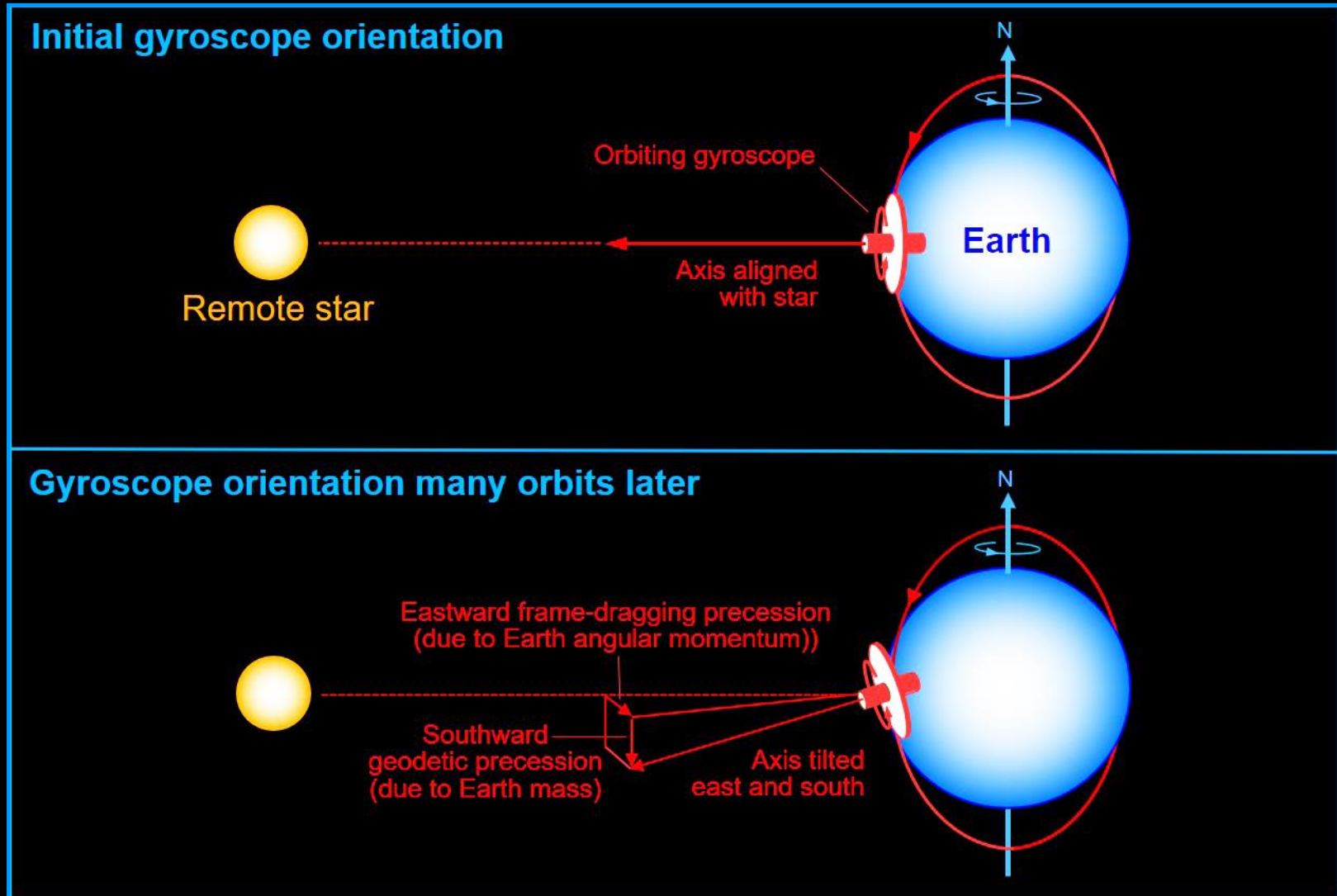
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- Predictions extracted from these gravitoelectromagnetic equations are claimed to agree with data collected by an orbiting satellite

# Gravitoelectromagnetism

## Precession of Orbiting Gyroscope



Not to scale. Geodetic precession much greater than frame-dragging precession. Confirmation claimed by Everitt et al, PRL 106, 221101 (2011) via the Gravity Probe B experiment (longest continuously funded science project in NASA history, begun in 1963). Actual gyroscope consisted of four spinning spheres, two of which malfunctioned during experiment, which greatly complicated data analysis

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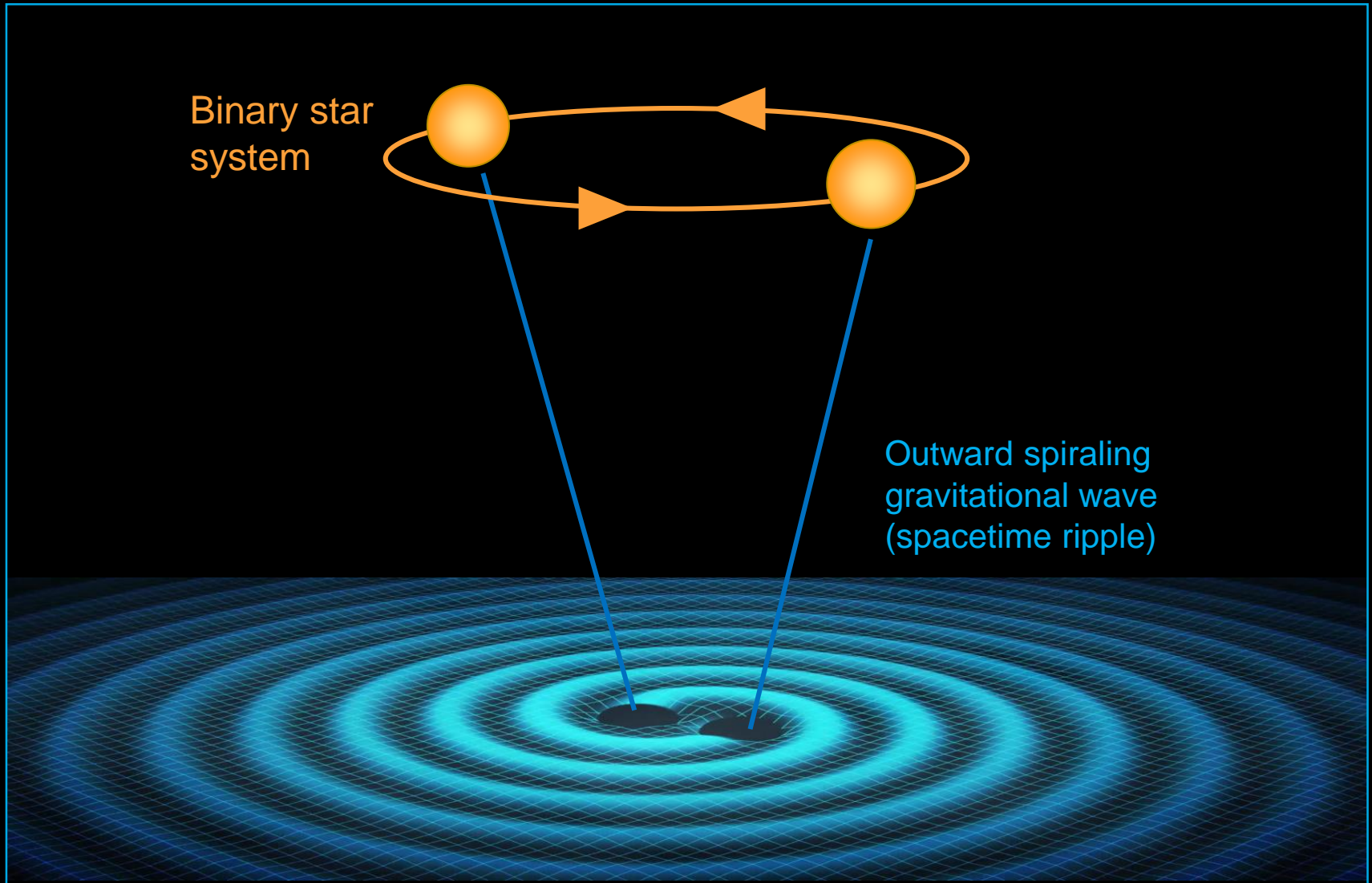
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# Gravitational Waves



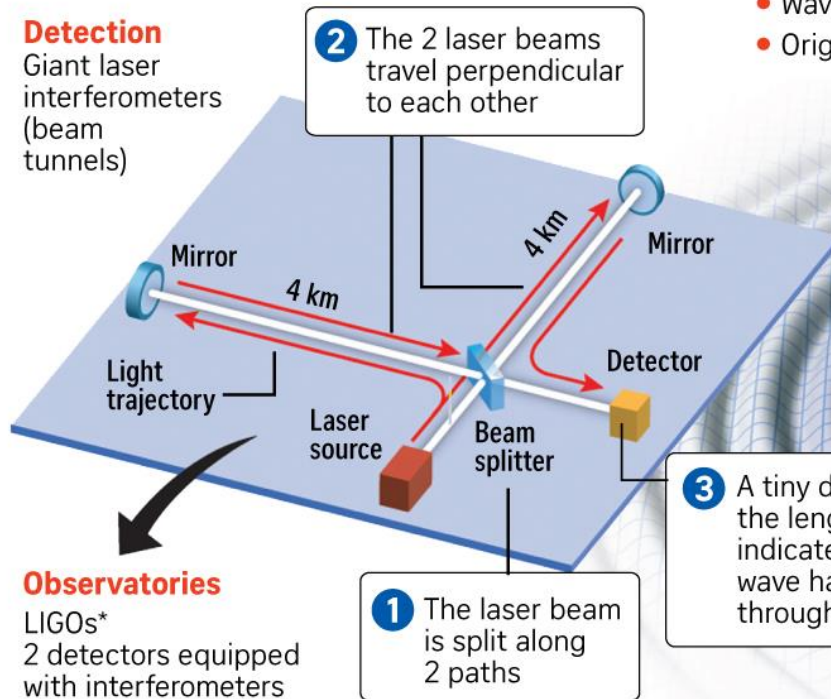
Einstein predicted such ripples in 1916. Detection (extremely difficult) took 100 years (next two slides)

# Gravitational waves observed directly for the first time

A major advancement that opens a window on the universe

## Detection

Giant laser interferometers (beam tunnels)



- Waves were detected Sept 14 at 16:51GMT
- Origin: fusion of 2 black holes 1.3 billion of years ago

## Observatories

LIGOs\*  
2 detectors equipped with interferometers



Albert Einstein predicted gravitational waves in 1916 in his General Theory of Relativity



Detection of gravitational waves makes it possible to work backwards to the first millisecond of the Big Bang

\*Laser Interferometer Gravitational Wave Observatories

# Observation of Gravitational Waves from a Binary Black Hole Merger

---

On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sweeps upwards in frequency from 35 to 250 Hz with a peak gravitational-wave strain of  $1.0 \times 10^{-21}$ . It matches the waveform predicted by general relativity for the inspiral and merger of a pair of black holes and the ringdown of the resulting single black hole. The signal was observed with a matched-filter signal-to-noise ratio of 24 and a false alarm rate estimated to be less than 1 event per 203,000 years. The source lies at a luminosity distance of 410 Mpc corresponding to a redshift  $z = 0.09$ . In the source frame, the initial black hole masses are  $36 M_{\odot}$  and  $29 M_{\odot}$ , and the final black hole mass is  $62 M_{\odot}$ , with  $3.0 M_{\odot} c^2$  radiated in gravitational waves. These observations demonstrate the existence of binary stellar-mass black hole systems. This is the first direct detection of gravitational waves and the first observation of a binary black hole merger.

Title and abstract verbatim from Abbott et al, *Physical Review Letters* **116**, 061102 (2016), except for omission of standard deviations to reduce clutter.  $M_{\odot}$  = Sun mass. 2017 Nobel Prize awarded to Rainer Weiss, Kip Thorne and Barry C. Barish



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# Thermodynamics

---

- Science of energy and entropy
- First law for isolated system: Energy is a constant (conserved)
- Second law for isolated system: Entropy cannot decrease
- Uniqueness of thermodynamics lies in the second law, which provides an "arrow of time." Isolated macroscopic systems "run down" and eventually experience a "heat death"
- Thermodynamics precludes existence of perpetual motion machines\*

\*Claims of such machines are automatically dismissed by the US Patent and Trademark Office

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# Thermodynamics – First & Second Laws

Exclude External Time-Varying Gravitational / Electromagnetic Fields

Closed System

Heat input ↓  $dQ$



$E$  = energy  
 $S$  = entropy

Work output ↓  $dW$

1st Law  $dE = dQ - dW$

2nd Law  $dS \geq dQ/T$   $T$  = system temperature where heat enters

Equal sign in reversible case

"Closed" means no  
mass in/out of system

# Thermodynamics – First & Second Laws

Exclude External Time-Varying Gravitational / Electromagnetic Fields

Closed System

Heat input ↓  $dQ$



Work output ↓  $dW$

Isolated System

$$dQ = 0$$



$$dW = 0$$

1st Law  $dE = dQ - dW$

$$E = \text{Const}$$

2nd Law  $dS \geq dQ/T$

$$dS \geq 0$$

"Closed" means no mass in/out of system

"Isolated" means no input/output of any kind

# Thermodynamics – First & Second Laws

Exclude External Time-Varying Gravitational / Electromagnetic Fields

Closed System

Heat input  $\downarrow$   $dQ$



Work output  $\downarrow$   $dW$

Isolated System

$$dQ = 0$$



$$dW = 0$$

Equilibrated System

$$dQ = 0$$



$$dW = 0$$

1st Law  $dE = dQ - dW$

$$E = \text{Const}$$

$$E = \text{Const}$$

2nd Law  $dS \geq dQ/T$

$$dS \geq 0$$

$$S = \text{Const} = \text{Max}$$

"Closed" means no mass in/out of system

"Isolated" means no input/output of any kind

"Equilibrated" means no longer changing

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What kinds of internal changes cause the entropy of a system to rise?



# Thermodynamics – Entropy Generation Density

Entropy generation-rate density for simple fluid at local equilibrium

$$\sigma = \frac{\overbrace{-\mathbf{q} \cdot \nabla \frac{1}{T}}^{\text{thermal conduction}} - \sum_i \overbrace{\mathbf{j}_i \cdot T \nabla \frac{\mu_i}{T}}^{\text{mass diffusion}} + \overbrace{\mathbf{j} \cdot (\mathbf{E} + \mathbf{v} \times \mathbf{B})}^{\text{electric current}} - \overbrace{\boldsymbol{\tau} : \boldsymbol{\varepsilon}}^{\text{friction}} - \sum_r \overbrace{R_r A_r}^{\text{reactions}}}{T}$$

Each term in the numerator consists of a thermodynamic flux-force product. Each thermodynamic flux (left) is driven by a thermodynamic force (right). Each product provides a positive contribution to the entropy generation rate density  $\sigma$  resulting from thermalization of energy

At overall equilibrium, when the fluxes have been driven to zero and all energy that can be thermalized has been thermalized, the entropy of the system is maximized

$\mathbf{q}$  = internal energy diffusion flux density,  $\nabla$  = gradient operator,  $T$  = absolute temperature,  $\mathbf{j}_i$  = chemical species  $i$  diffusion flux density,  $\mu_i$  = species  $i$  chemical potential,  $\mathbf{j}$  = conduction current density,  $\mathbf{E}$  = electric field,  $\mathbf{v}$  = fluid velocity,  $\mathbf{B}$  = magnetic field,  $\boldsymbol{\tau}$  = shear stress tensor,  $\boldsymbol{\varepsilon}$  = strain rate tensor,  $R_r$  = rate of chemical reaction  $r$ ,  $A_r$  = affinity of chemical reaction  $r$

The End